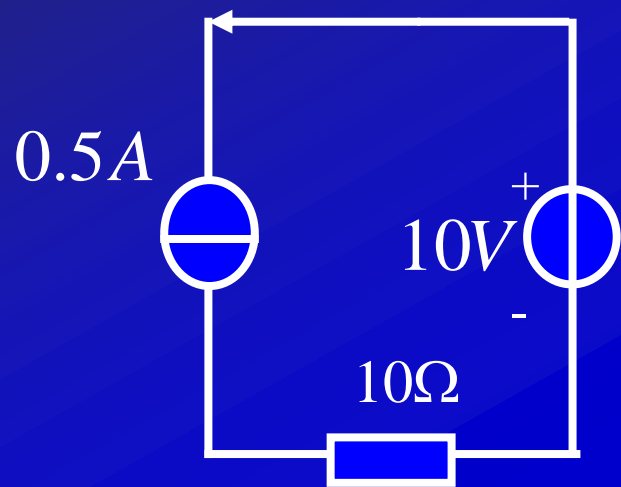


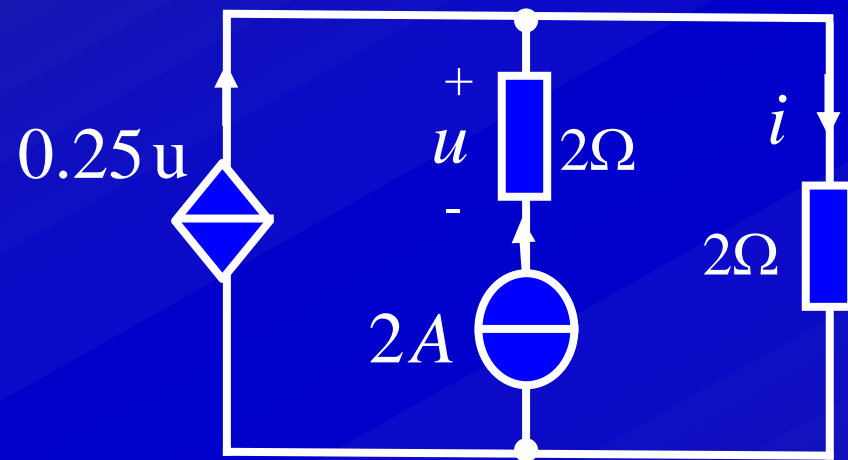
参考方向如下图，求电阻端电压U及电流源的功率。



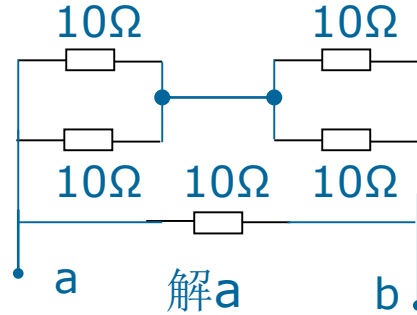
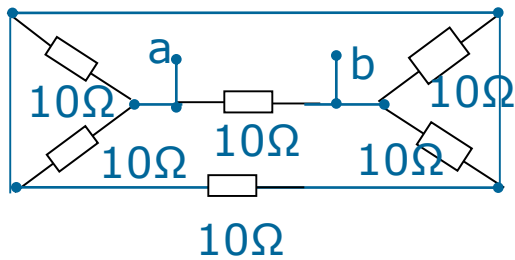
$$P_U = -I_s U_s = -5W$$

$$P_I = I_s (U_s - RI_s) = 2.5W$$

求电流 i

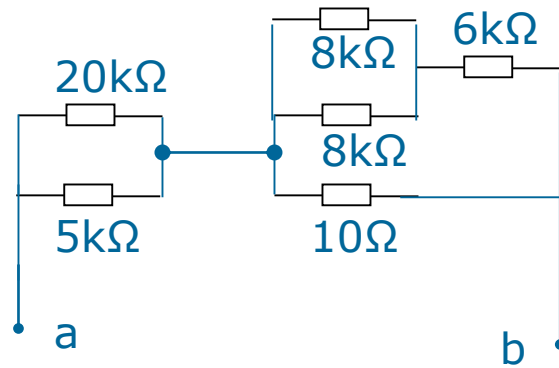
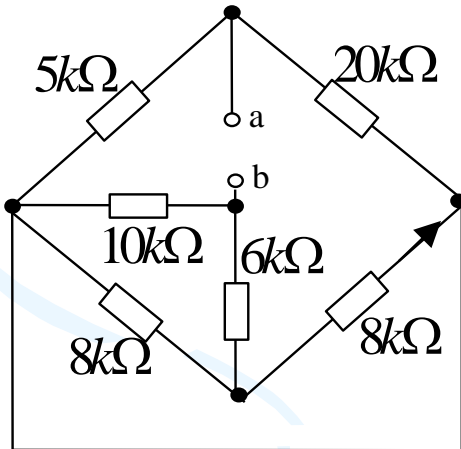


2-6 试求题图2-6中各电路a、b端间的等效电阻。



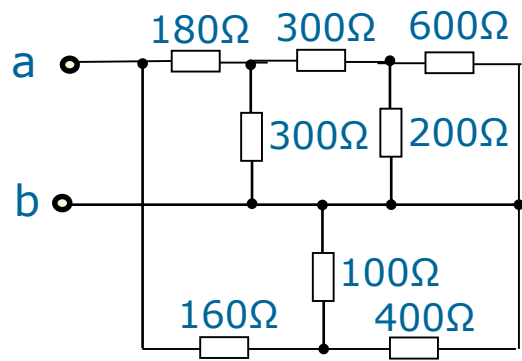
解: (a)原电路可等效为解a所示电路, 由图可得

$$R_{ab} = 10 // [10 // 10 + 10 // 10] = 5\Omega$$



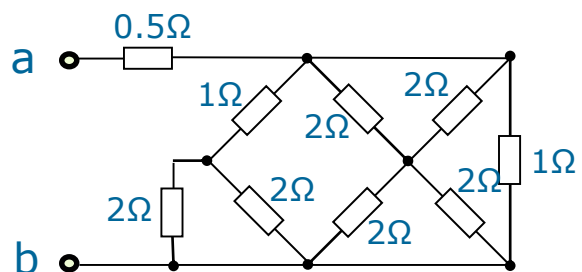
题图 2-6(b)

(b)由图可得: $R_{ab} = 5 // 20 + 10 // [8 // 8 + 6] = 9k\Omega$



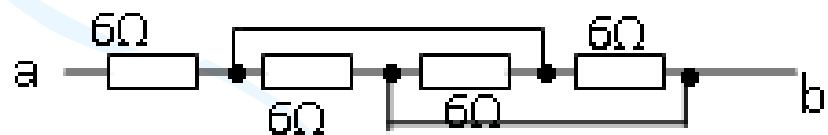
(c)

$$R_{ab} = [160 + 100 // 400] // \{180 + 300 // [300 + 600 // 200]\} = 144\Omega$$



(d)

$$R_{ab} = 0.5 + [(1 + 2 // 2) // (2 // 2 + 2 // 2) // 1] = 1\Omega$$



(e)

$$R_{ab} = 6 + 6 // 6 // 6 = 8\Omega$$

2-10 电路如题图2-10所示, (1)若 $U_2=10V$, 求电流 I_1 和电源电压 U_s ; (2)若 $U_s=10V$, 求电压 U_2 。

解: (1) $I_2 = \frac{U_2}{20} = 0.5A$

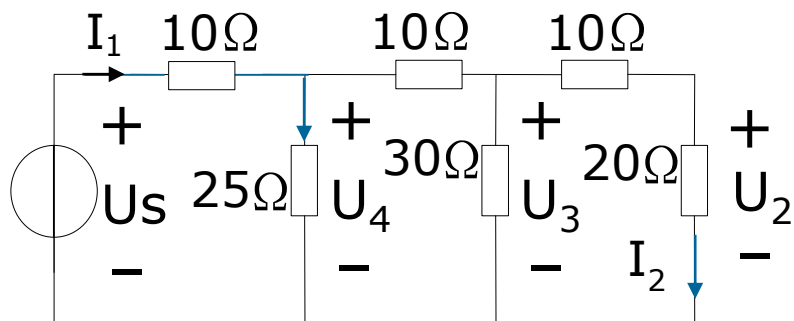
$$U_3 = I_2(10 + 20) = 15V$$

$$U_4 = \left(\frac{U_3}{30} + I_2 \right) \times 10 + U_3 = 25V \quad \therefore I_1 = \frac{U_4}{25} + \frac{U_3}{30} + I_2 = 2A$$

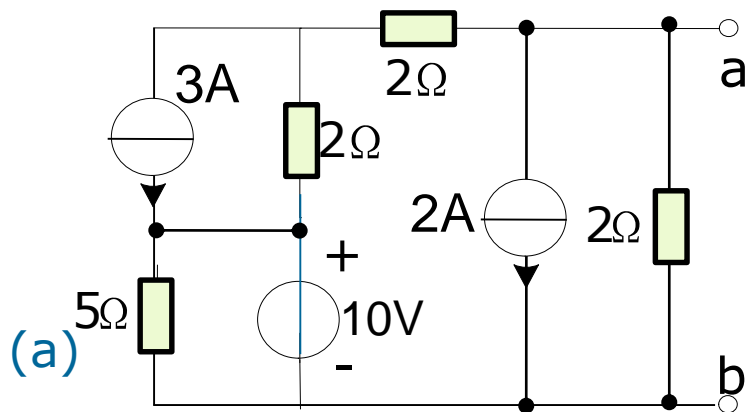
$$U_s = I_1 \times 10 + U_4 = 45V$$

(2) $I_1 = \frac{U_s}{10 + 25 // [10 + 30 // (10 + 20)]} = \frac{10}{22.5} A$

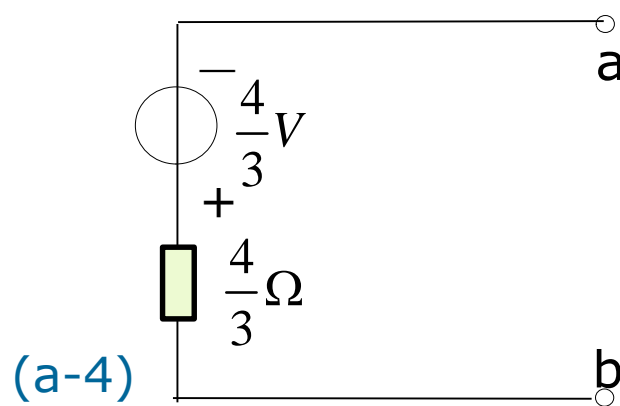
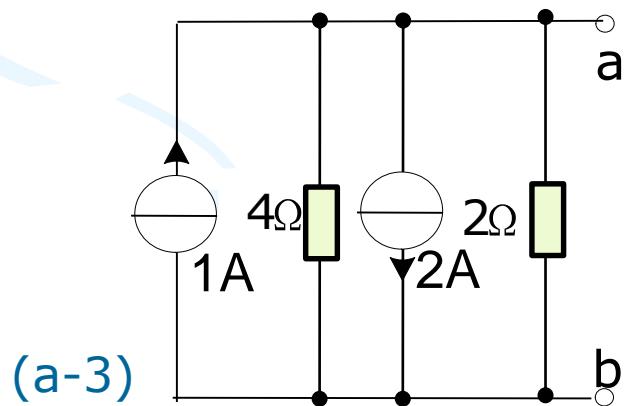
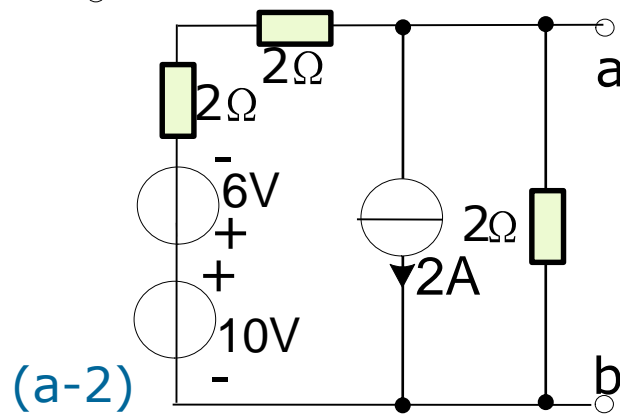
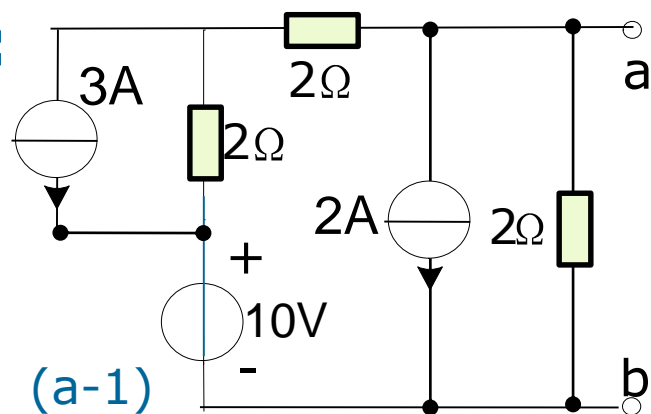
$$\begin{aligned} \therefore I_2 &= \frac{10}{22.5} \times \frac{25}{25 + [10 + 30 // (10 + 20)]} \times \frac{25}{30 + 10 + 20} = \frac{10}{22.5} \times \frac{1}{2} \times \frac{1}{2} \\ &= \frac{1}{9} A \end{aligned}$$



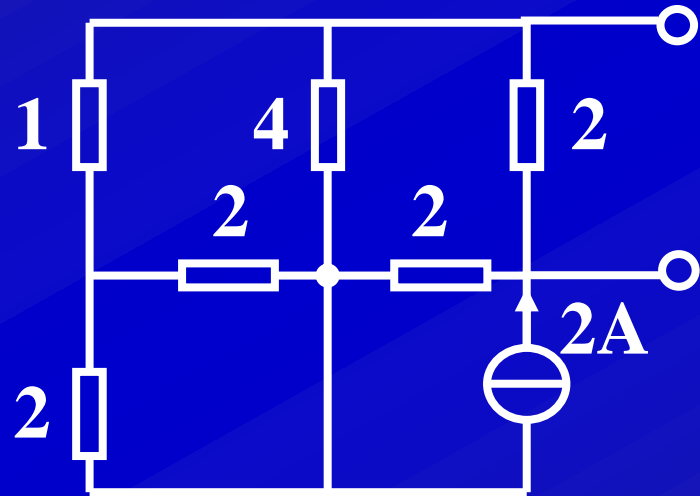
2-15(a) 化简题图2-15所示电路为等效戴维南电路。



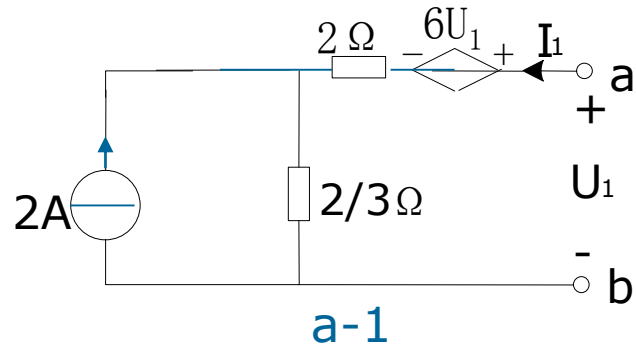
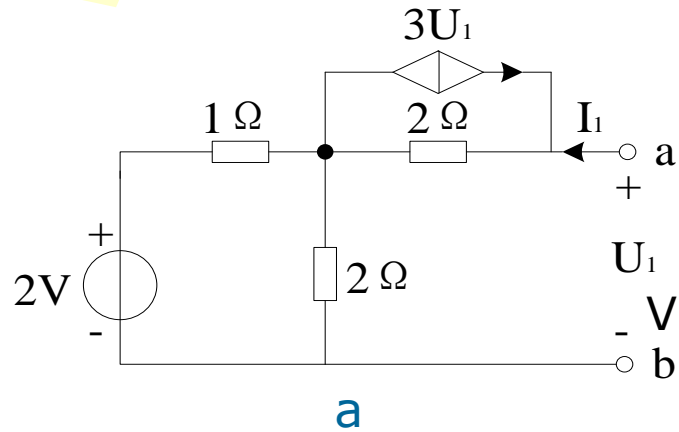
解:



化简



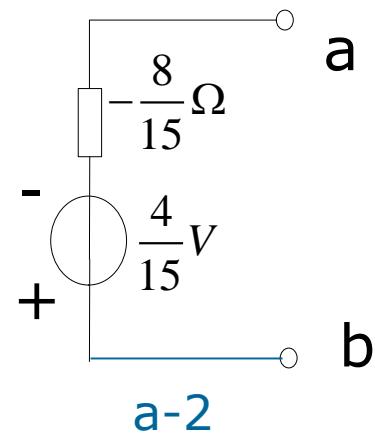
2-24(a) 化简题图2-24所示电路为等效戴维南电路。



解(a): 首先将图a所示电路等效化简为图a-1所示电路, 设端口上电压、电流参考方向如图, 则:

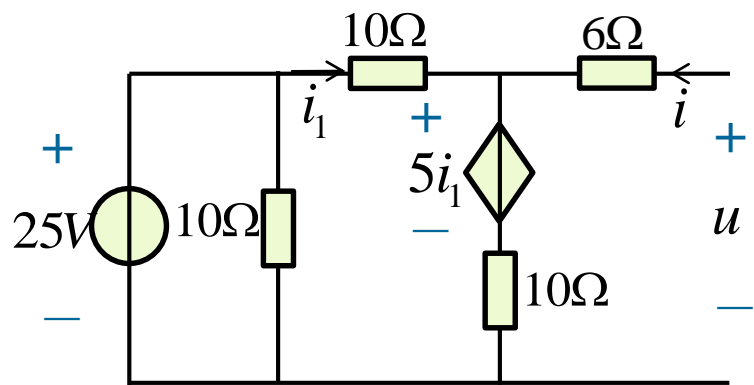
$$U_1 = 6U_1 + 2I_1 + \frac{2}{3}(2 + I_1)$$

$$\therefore U_1 = -\frac{4}{15} - \frac{8}{15}I_1$$



所以戴维南等效电路如图a-2所示。

2-24(b) 化简题图2-24所示电路为等效戴维南电路。

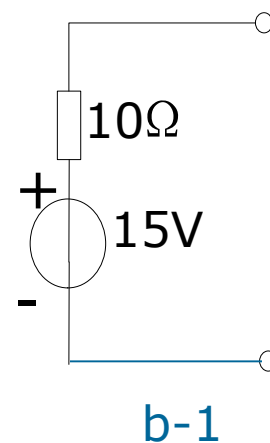


解：设端口电压、电流的参考方向如图，则：

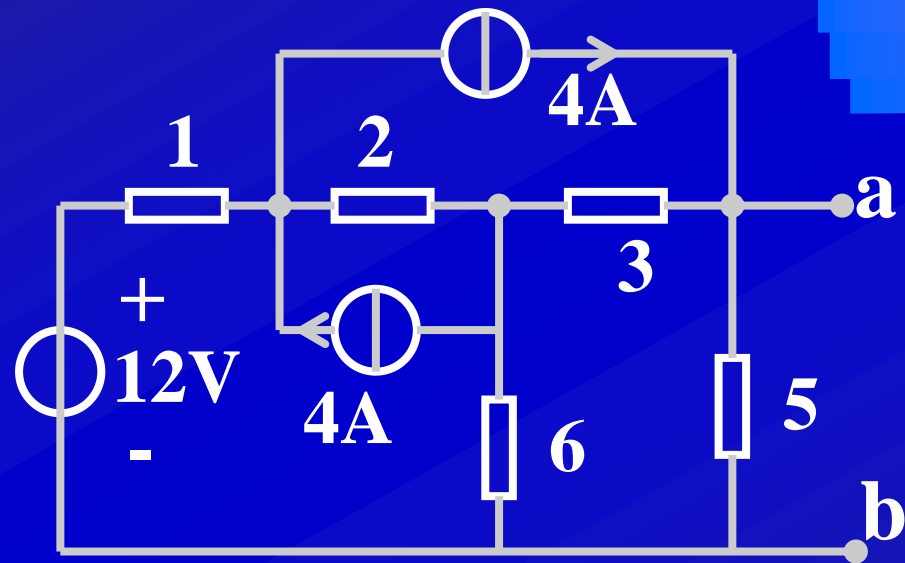
$$\begin{cases} u = 6i - 10i_1 + 25 \\ u = 6i + 5i_1 + 10(i_1 + i) \end{cases}$$

消去 i_1 ，有： $u = 10i + 15$

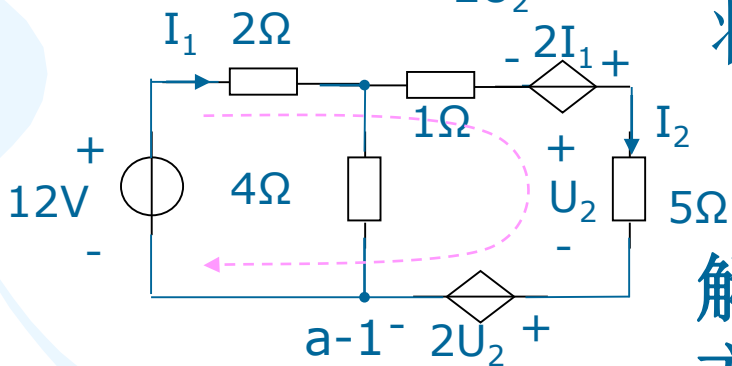
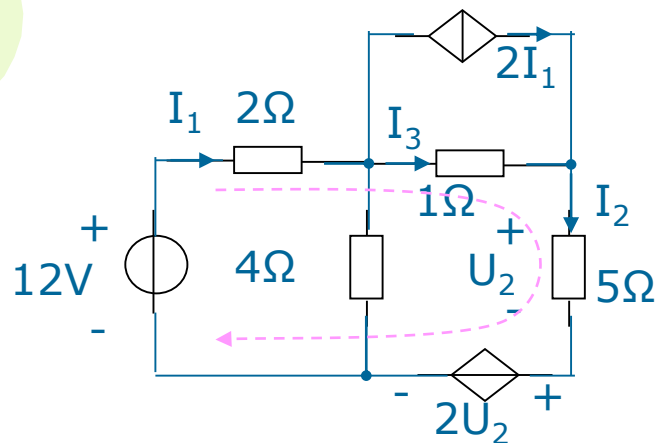
所以戴维南等效电路如图b-1所示



化简



2-27 试求题图2-27电路中的电流 I_2 。



解一：先将原电路进行等效变换如图**b-1**，列图示回路**KVL**方程，有：

$$2I_1 + I_2 \times 1 - 2I_1 + 5I_2 + 2U_2 - 12 = 0$$

将 $U_2 = 5I_2$ 代入上式，可得：

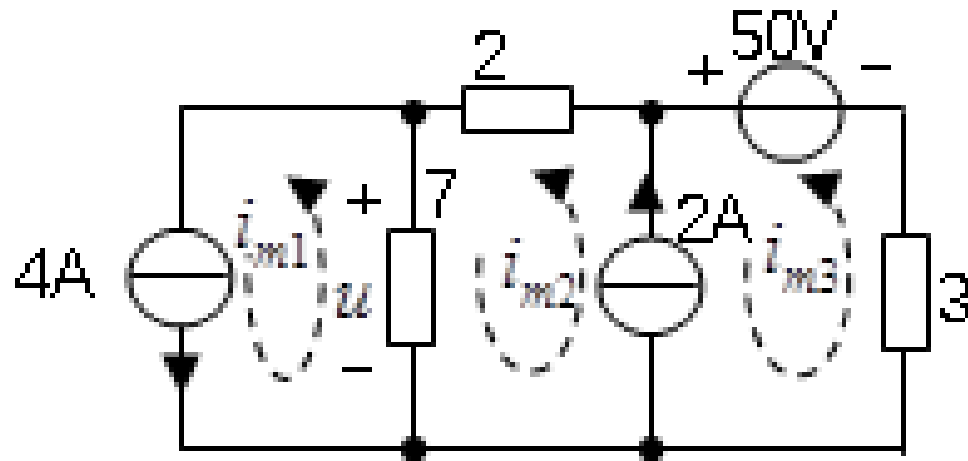
$$I_2 = 0.75A$$

解二：在原电路上列图示回路**KVL**方程，有：

$$2I_1 + I_3 \times 1 + 5I_2 + 2U_2 - 12 = 0$$

将 $I_3 = I_2 - 2I_1$, $U_2 = 5I_2$ 代入上式，可得： $I_2 = 0.75A$

用网孔分析法求解题图所示电路中的电压 u 。



$$\begin{cases} i_{m1} = 4 \\ -7i_{m1} + 12i_{m2} - 3i_{m3} = 50 \\ i_{m3} = 2 \\ u = 7(i_{m2} - i_{m1}) \end{cases}$$

$$\therefore u = 21V$$

列节点方程

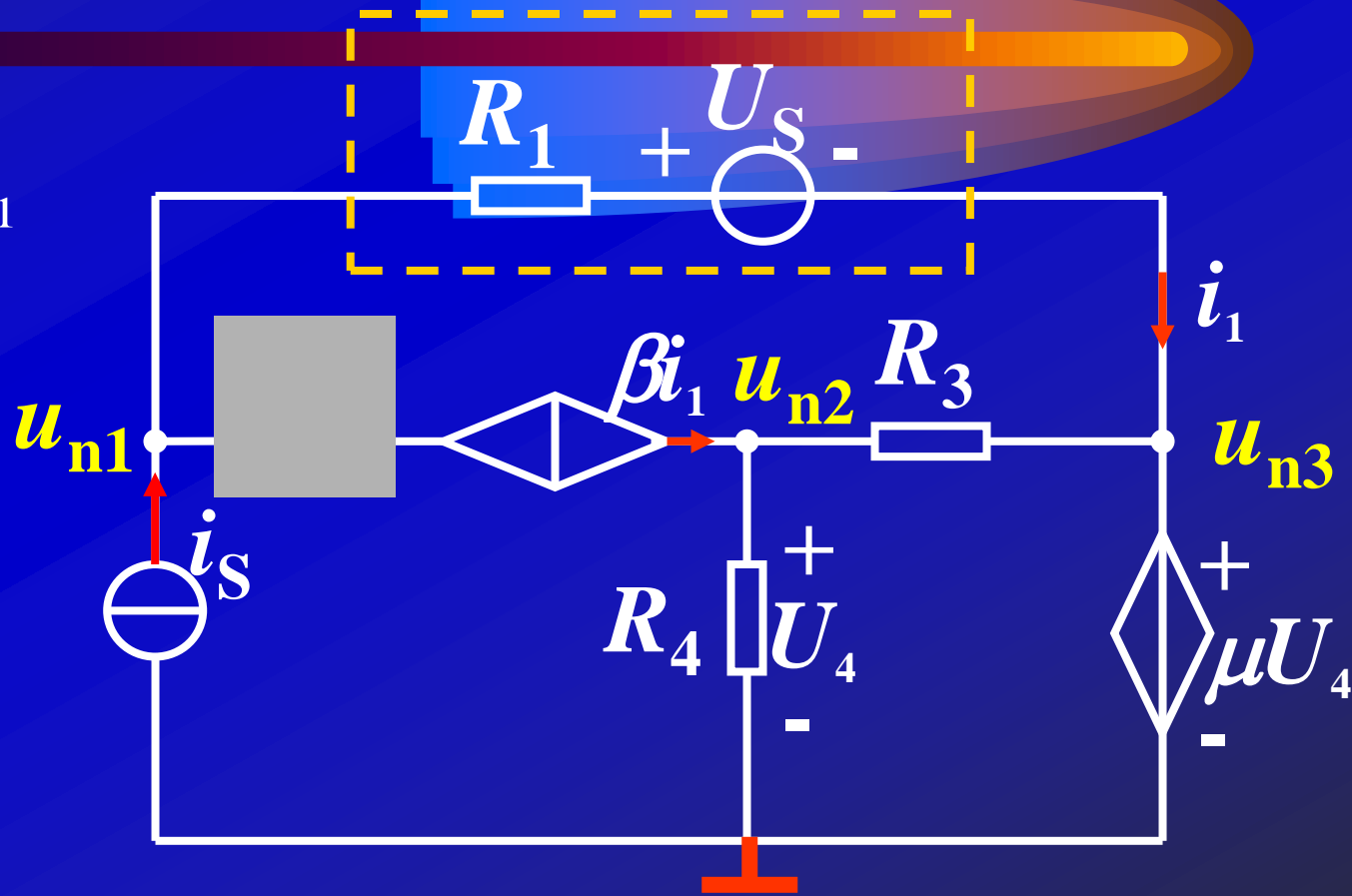
$$\frac{1}{R_1} u_{n1} - \frac{1}{R_1} u_{n3} = \frac{U_S}{R_1} + i_S - \beta i_1$$

$$\left(\frac{1}{R_3} + \frac{1}{R_4}\right) u_{n2} - \frac{1}{R_3} u_{n3} = \beta i_1$$

$$u_{n3} = \mu u_{n4}$$

$$i_1 = \frac{1}{R_1} (u_{n1} - u_{n3} - U_S)$$

$$U_4 = u_{n2}$$

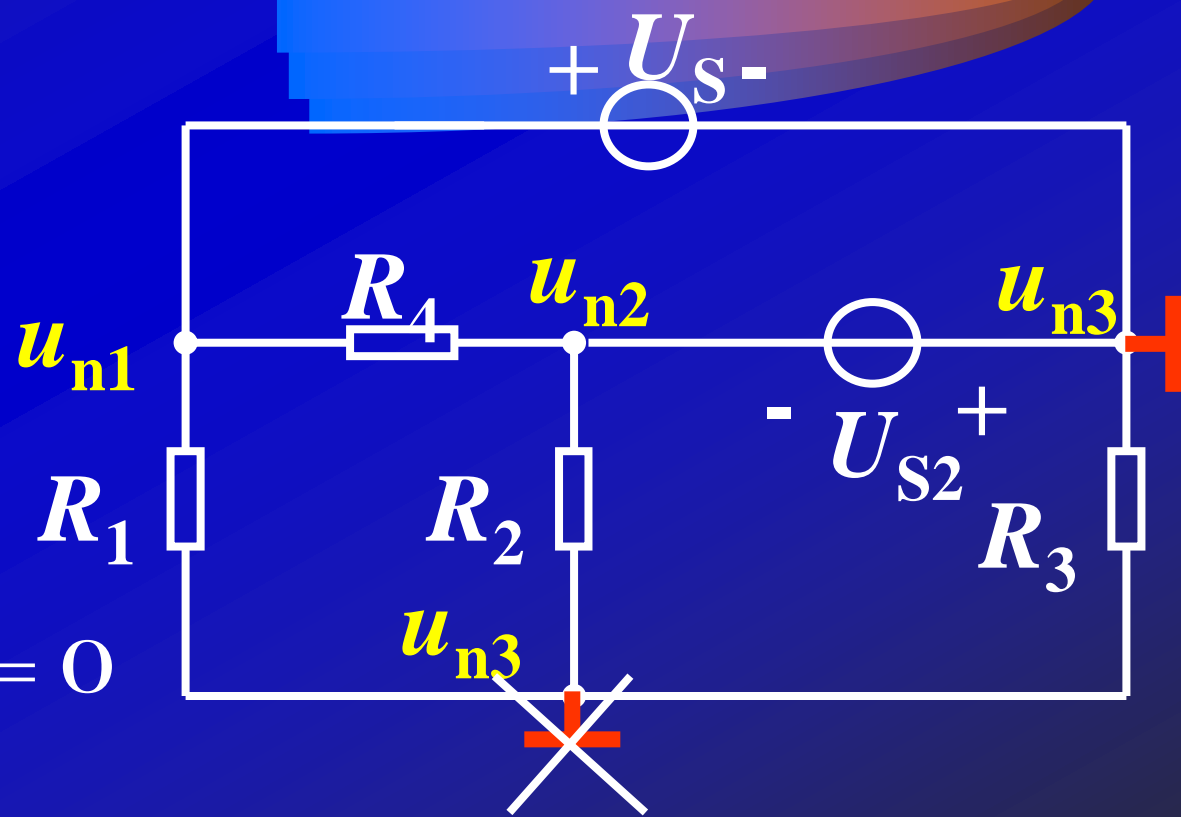


列节点方程

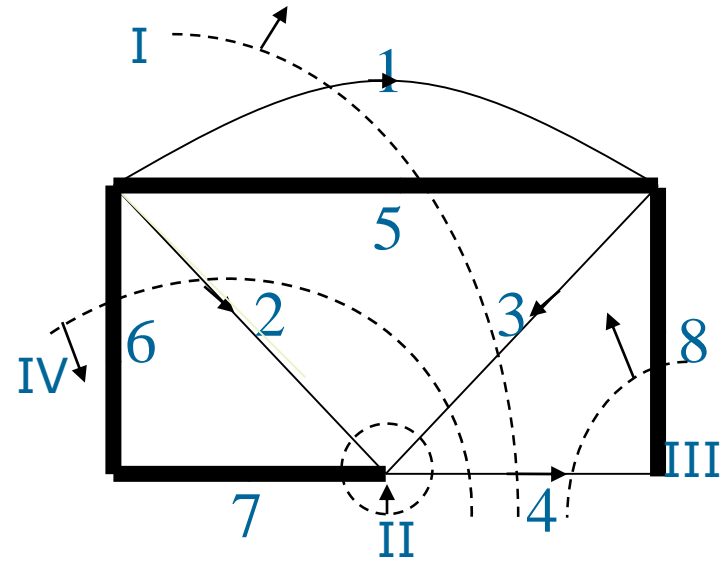
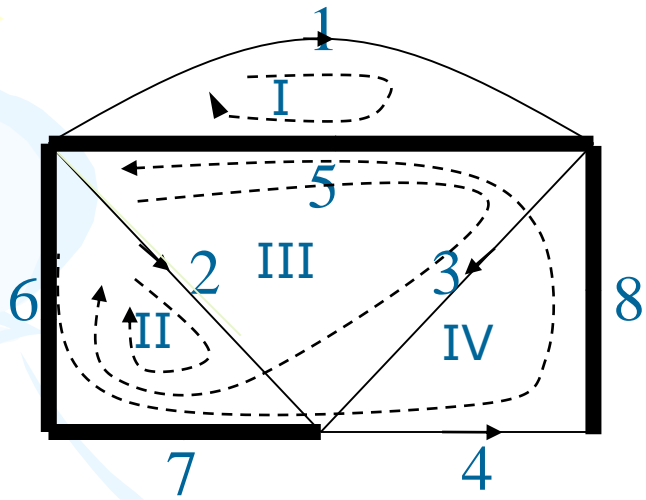
$$u_{n1} = U_S$$

$$u_{n2} = -U_{S2}$$

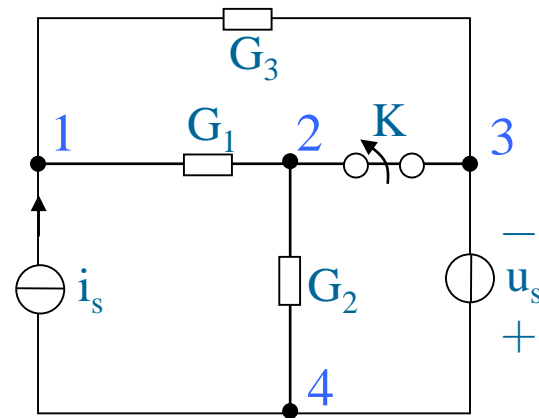
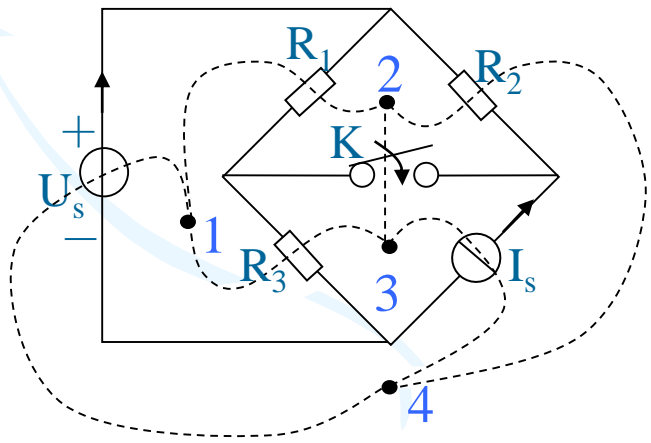
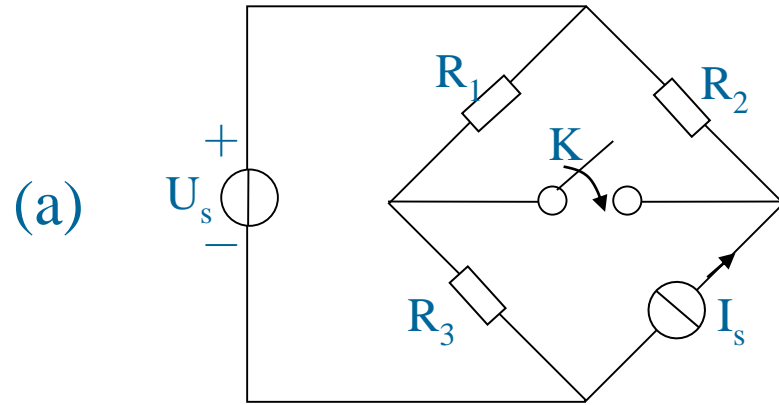
$$-\frac{1}{R_1}u_{n1} - \frac{1}{R_2}u_{n2} + \left(\frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3}\right)u_{n3} = 0$$



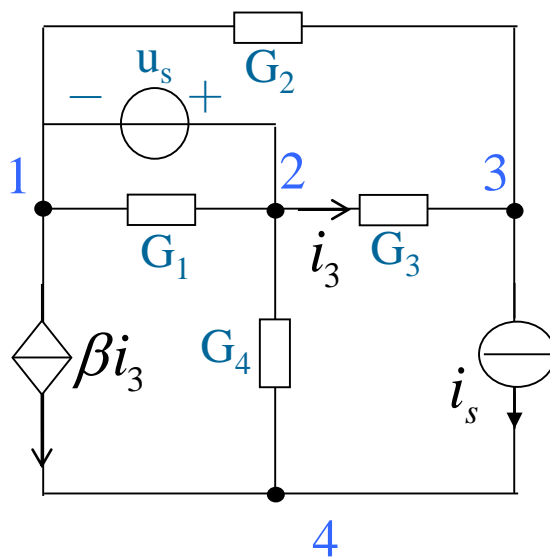
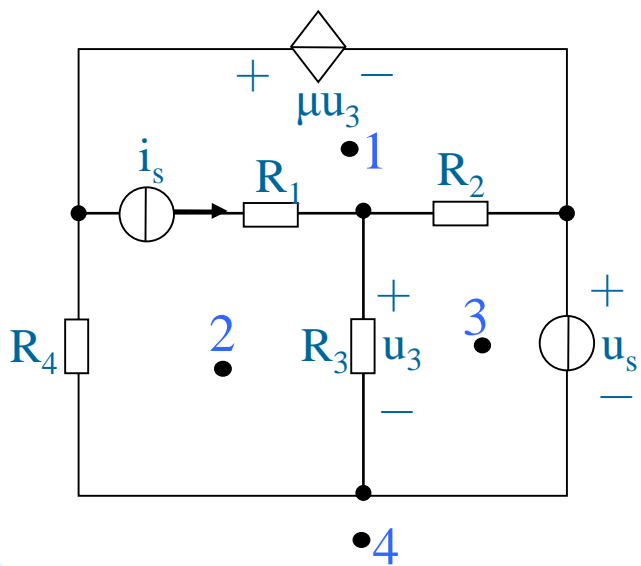
3-15、线图如图所示，粗线表示树，试列出其全部基本回路和基本割集。



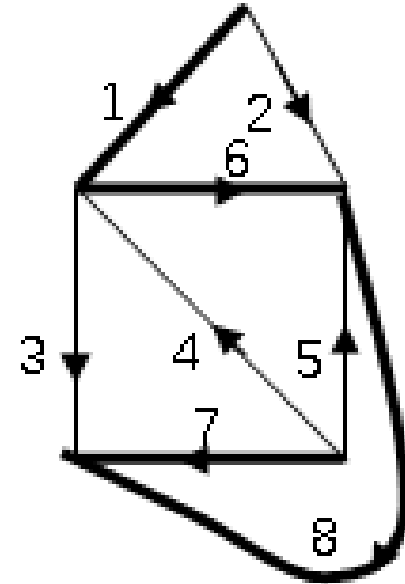
3-20、画出下图电路的对偶电路



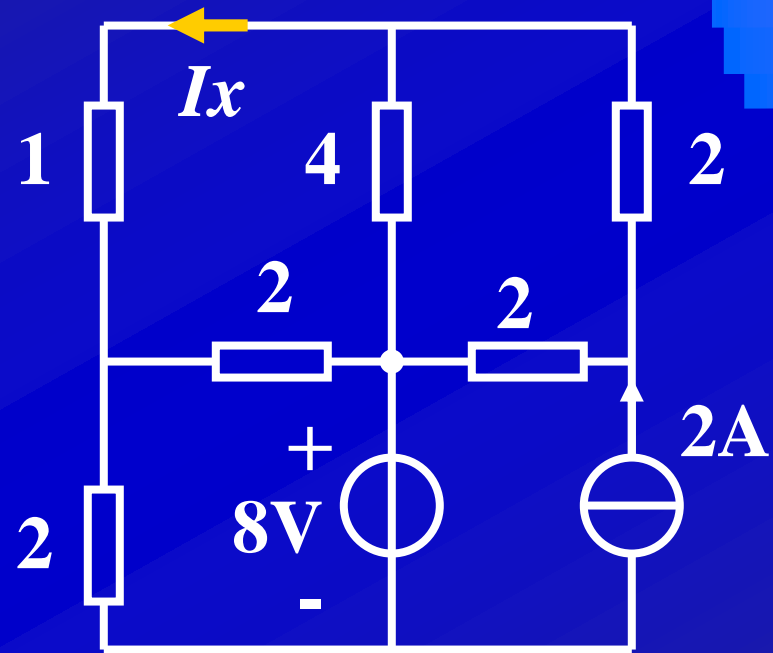
(b)

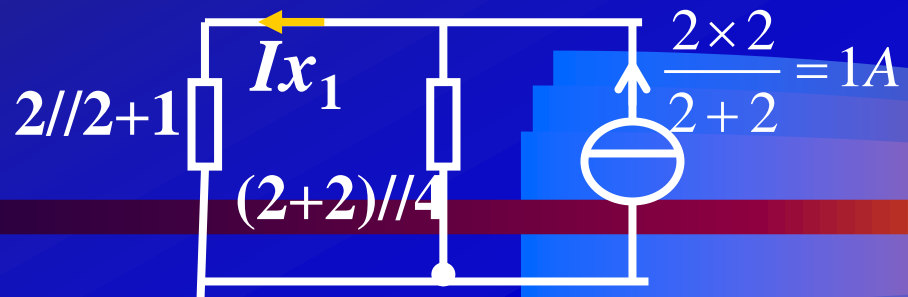
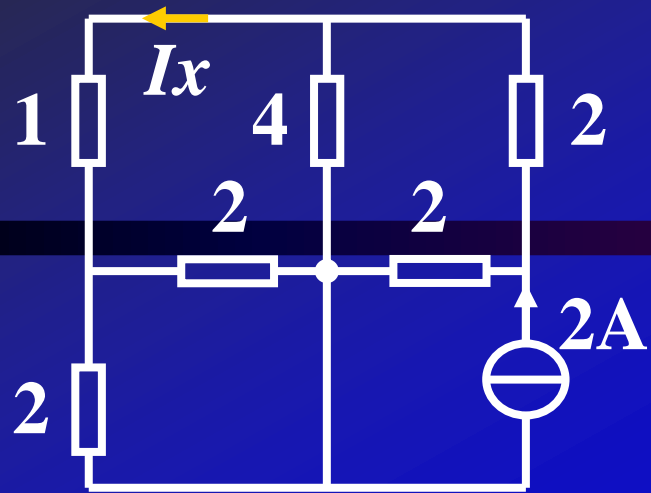


线图如题图，粗线表示树，画出下图电路的全部基本回路和基本割集。



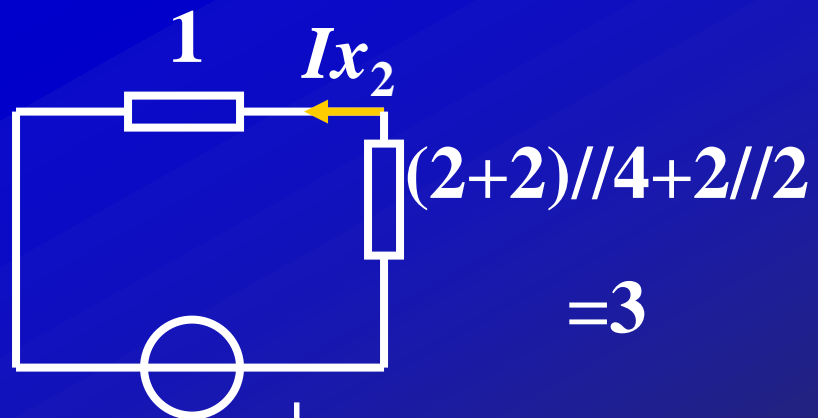
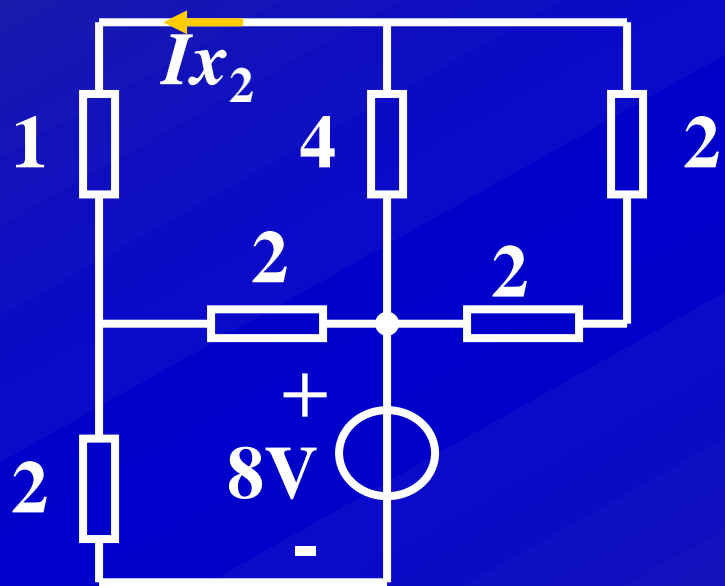
求电流 i_x





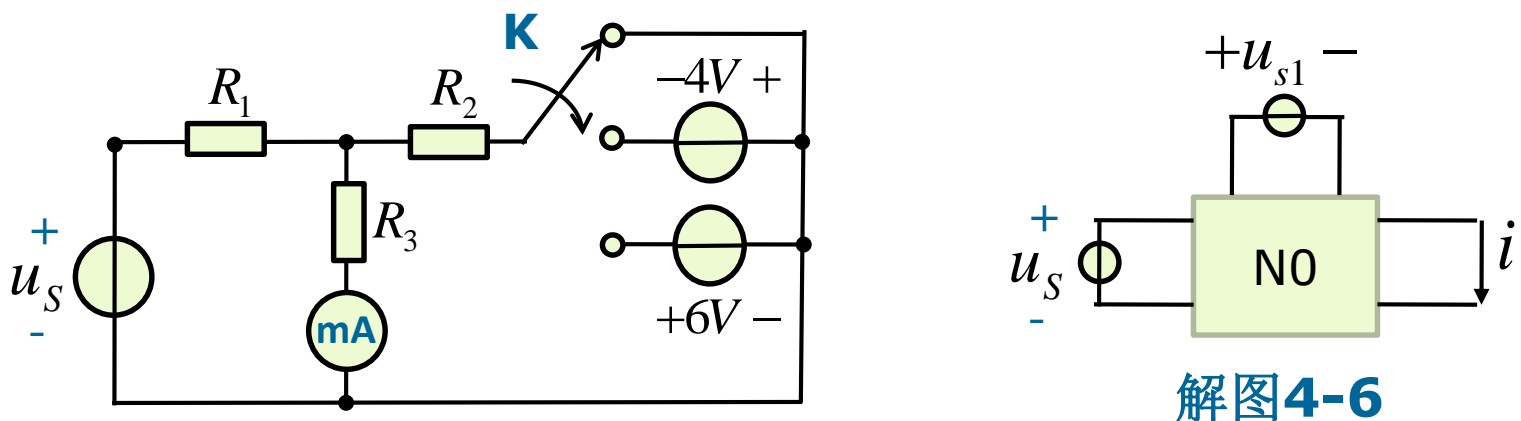
$$I_x = I_{x_1} + I_{x_2}$$

$$= 0.5 + 1 = 1.5A$$



$$\frac{8}{2} \times \frac{2}{2} = 4V$$

4-6 如题图4-6所示电路，当开关K合在位置1时电流表读数为40mA；当K合在位置2时，电流表读数为-60mA。试求K合在位置3时电流表的读数。



解图4-6

解：设N0为R1、R2和R3构成的线性无源网络，而*i*为电流表的读数，则有：
$$i = k_1 u_S + k_2 u_{S1} = 40 + 25 u_{S1}$$

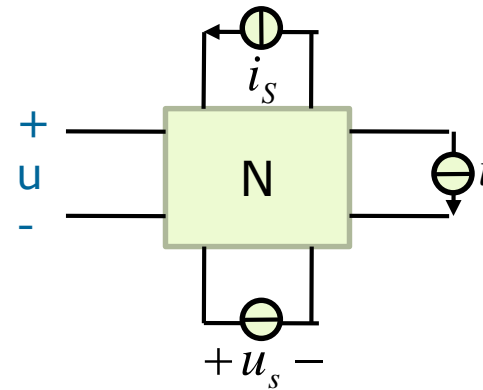
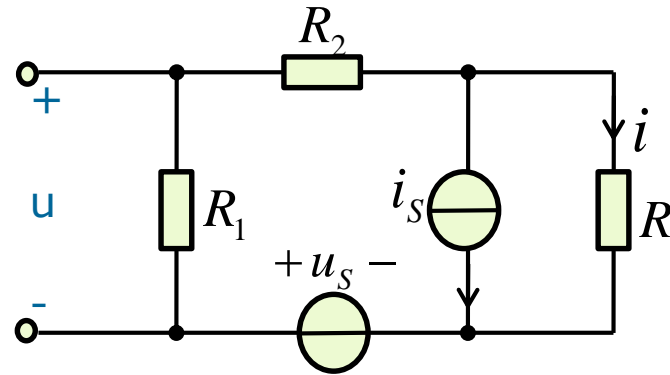
代入条件： $u_{S1} = 0V, i = 40mA; u_{S1} = -4V, i = -60mA$

则有：

$$\begin{cases} 40 = k_1 u_S + k_2 \times 0 \\ -60 = k_1 u_S + k_2 \times (-4) \end{cases} \Rightarrow k_2 = 25, k_1 u_S = 40$$

$$\therefore i = 40 + 25 \times 6 = 190mA$$

4-8 如题图4-8所示电路，当改变电阻R值时，电路中各处电压和电流都将随之改变，已知当 $i = 1A$ 时， $u = 20V$ ；当 $i = 2A$ 时， $u = 30V$ ；求当 $i = 3A$ 时，电压u为多少？



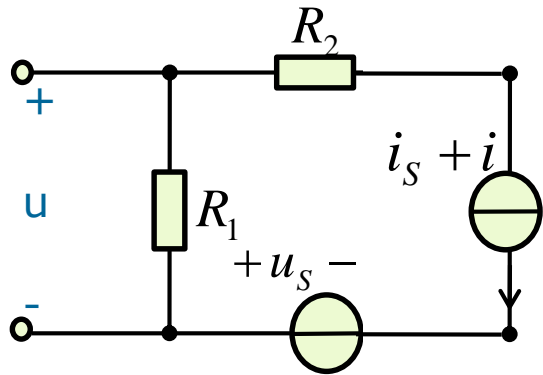
解：根据替代定理，可变电阻支路用电流源替代，根据线性网络的齐次性和叠加性，可设：

$$u = k_1 u_s + k_2 i_s + k_3 i$$

代入条件，则： $k_1 u_s + k_2 i_s + k_3 = 20$ $\therefore k_3 = 10$

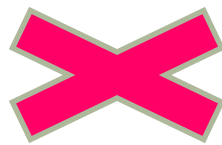
$$k_1 u_s + k_2 i_s + 2k_3 = 30 \quad k_1 u_s + k_2 i_s = 10$$

故当 $i = 3A$ 时： $u = 10 + 10 \times 3 = 40V$



错解： 根据替代定理有：

$$u = (i_s + i)R_1$$



代入条件，有： $(i_s + 1)R_1 = 20$

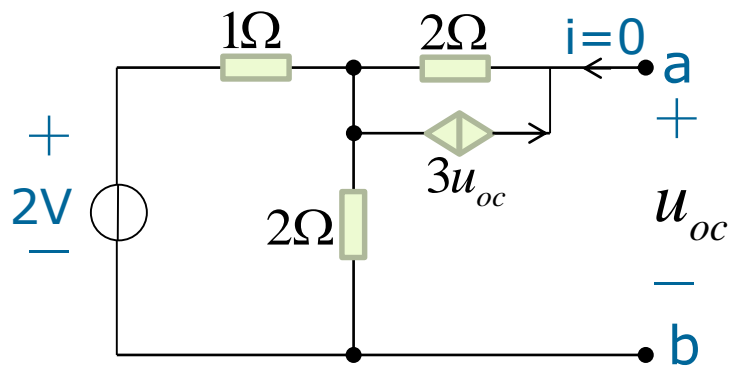
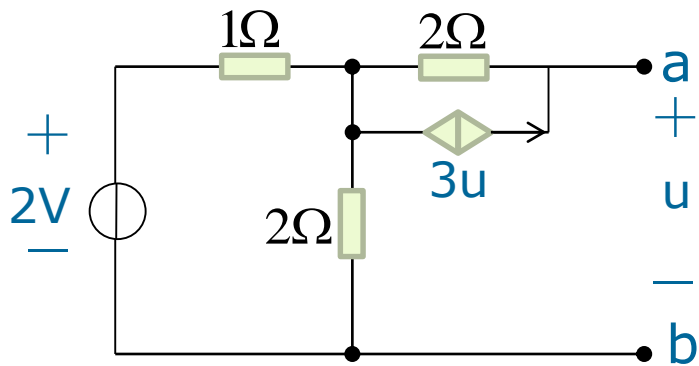
$$(i_s + 2)R_1 = 30$$

$$i_s = 1\text{A}, R_1 = 10\Omega$$

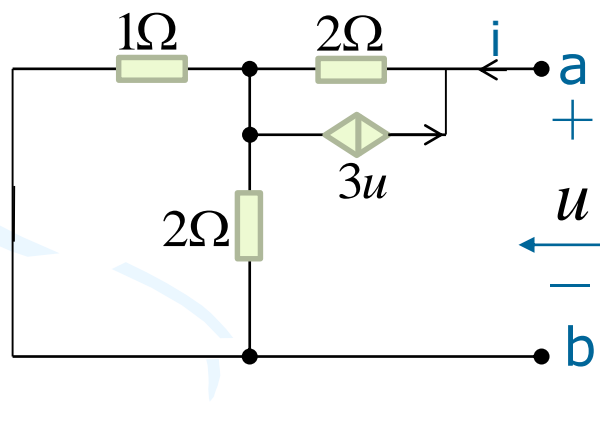
故，当 $i = 3\text{A}$

$$u = (i_s + i)R_1 = 40\text{V}$$

4-9(b). 试求题图4-9所示二端网络的戴维南等效电路。

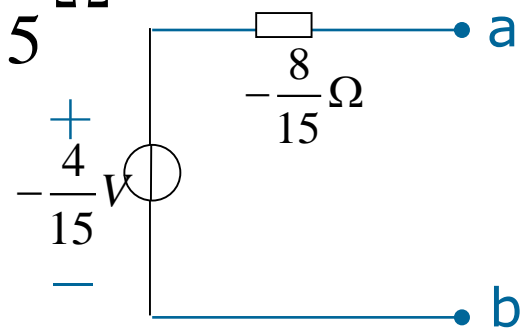


$$u_{oc} = 2 \times 3u_{oc} + 2 \times \frac{2}{1+2} \Rightarrow u_{oc} = -\frac{4}{15} \text{ V}$$

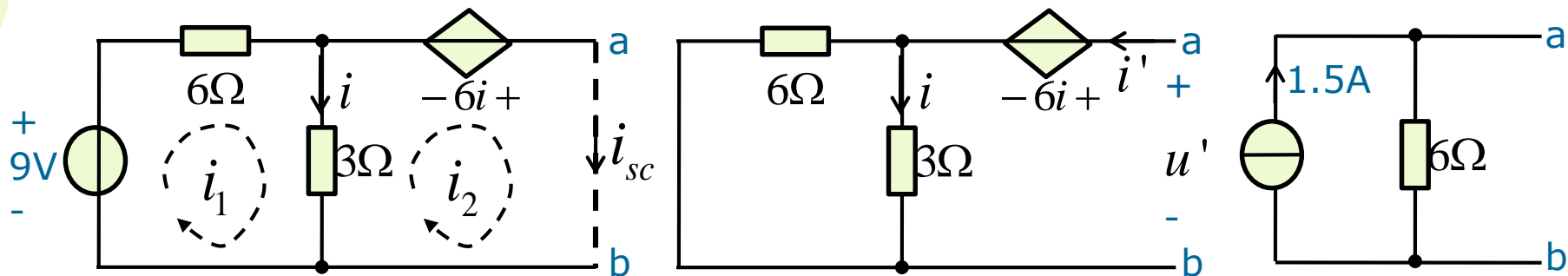


$$u = 2 \times (3u + i) + \frac{1 \times 2}{1+2} \times i$$

$$R_0 \therefore R_0 = \frac{u}{i} = -\frac{8}{15} \Omega$$



4-10(b) 试求题图4-10所示二端网络诺顿等效电路。



解： (1) 先求短路电流 i_{sc} ：令端口ab短路, 网孔法有：

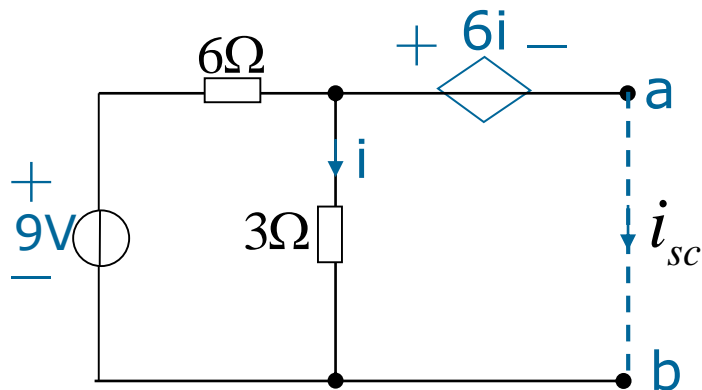
$$\begin{cases} 9i_1 - 3i_2 = 9 \\ -3i_1 + 3i_2 = 6i \\ i = i_1 - i_2 \end{cases} \quad \therefore i_{sc} = i_2 = 1.5A$$

(2) 求输出电阻 R_0 ：令独立电压源短路：

$$\begin{cases} u' = 6i + 3i = 9i \\ i = \frac{6}{6+3}i' \end{cases} \quad \therefore u' = 9 \times \frac{6}{6+3}i' = 6i'$$

$$R_0 = 6\Omega$$

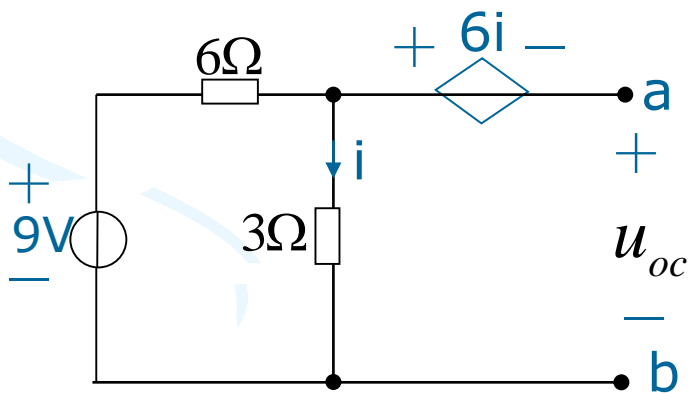
另解1: (1) 先求短路电流 i_{sc} :



$$\because 6i = -3i \quad \therefore i = 0$$

$$\therefore i_{sc} = \frac{9}{6} = 1.5A$$

另解2: (1) 先求短路电流 i_{sc} , 方向为 $a \rightarrow b$:

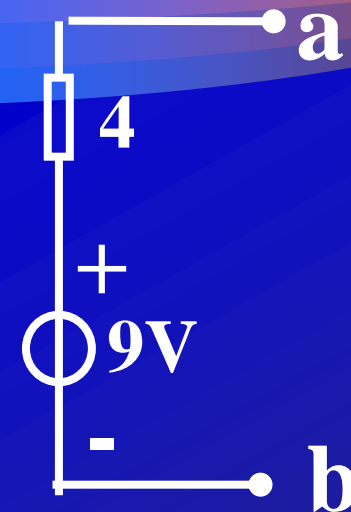
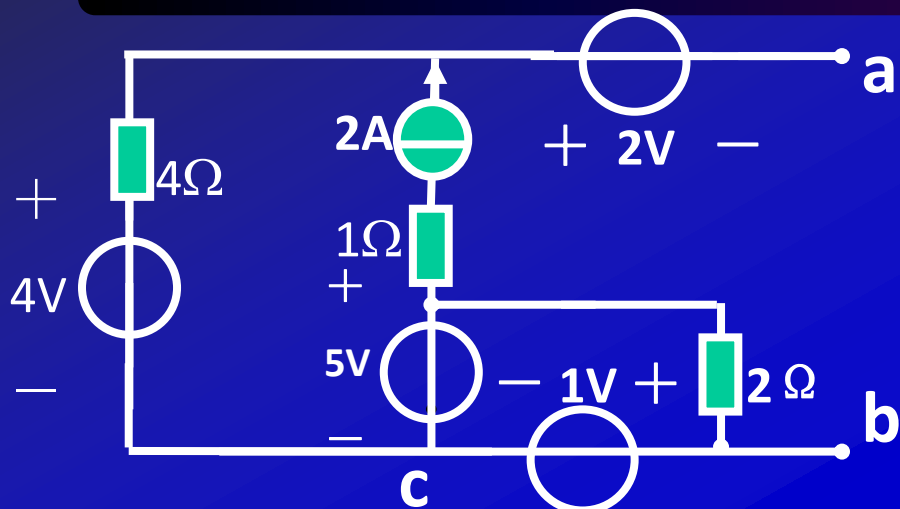


$$u_{oc} = 6i + 3i = 9i$$

$$i = \frac{9}{6+3} = 1A$$

$$\therefore i_{sc} = \frac{u_{oc}}{R_0} = 1.5A$$

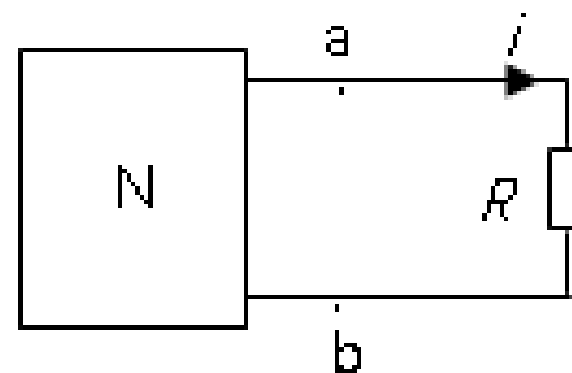
化简



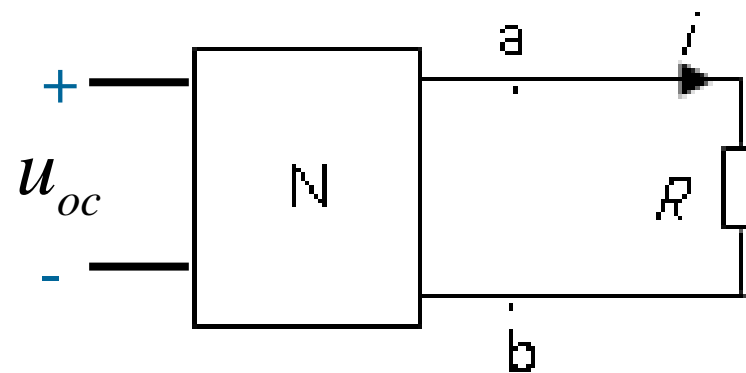
$$U_{OC} = -2 + 2 \times 4 + 4 - 1 = 9V$$

$$R_0 = 4\Omega$$

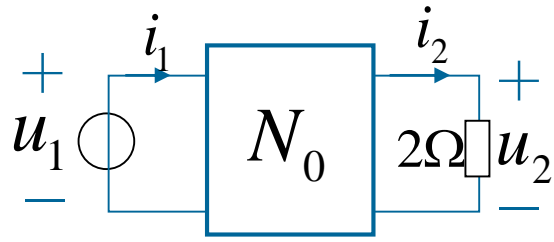
电路中N为含源线性网络，当 $R=5\Omega$ 时， $i=10\text{A}$ ；当 $R=15\Omega$ 时， $i=5\text{A}$ ；试求 $R=20\Omega$ 时， $i=?$



电路中N为含源线性网络，当改变外接电阻 R 时，电路中各处电压和电流将随之改变。当 $i = 1\text{A}$ 时， $u_{oc} = 6\text{V}$ ；当 $i = 2\text{A}$ 时， $u_{oc} = 10\text{V}$ ；试求当 $i = 5\text{A}$ 时， $u_{oc} = ?$

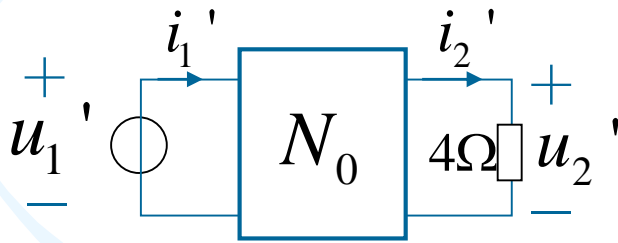


4-17 题图4-17中 N_0 为无源线性网络，只含电阻。当 $R_2 = 2\Omega, u_1 = 6V$ 时， $i_1 = 2A, u_2 = 2V$ 。试求当 R_2 改为 $4\Omega, u_1 = 10V$ 时，测得 $i_1 = 3A$ 情况下的电压 u_2 为多少？



解：作 $R_2 = 4\Omega$ 时的电路如解图4-17：

$$\because \sum u_k i'_k = \sum u'_k i_k$$



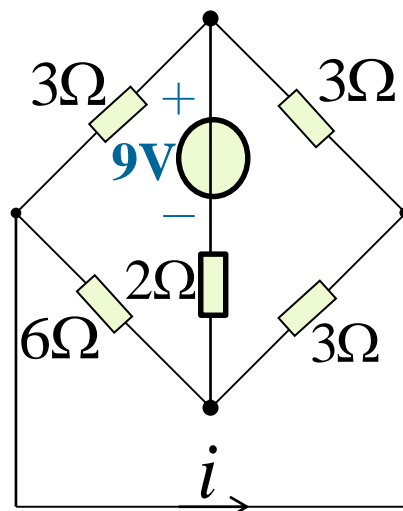
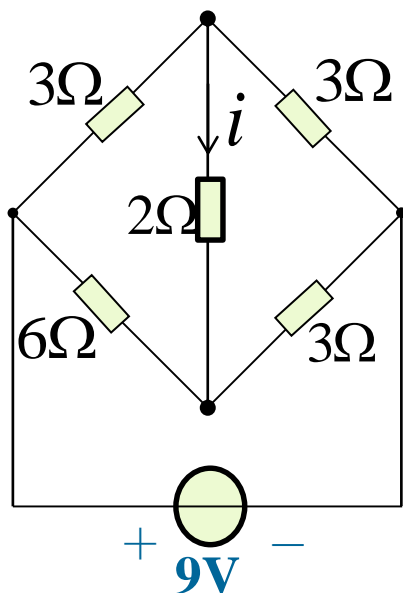
解图4-17

$$\therefore -u_1 i'_1 + u_2 i'_2 = -u'_1 i_1 + u'_2 i_2$$

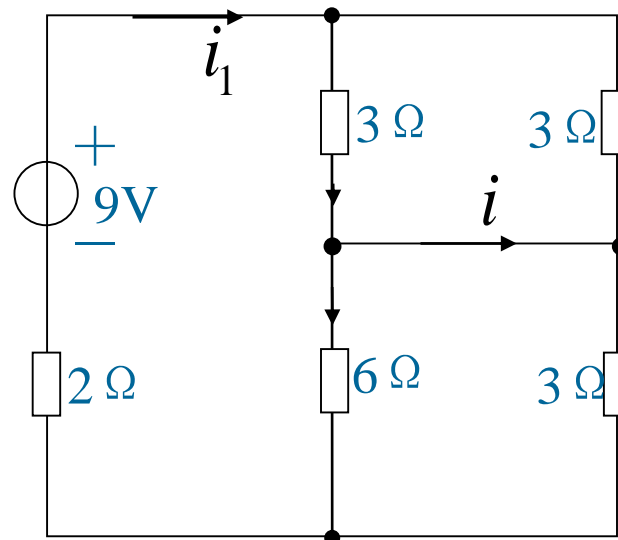
$$\therefore -6 \times 3 + 2 \times i'_2 = -10 \times 2 + u'_2 \times i_2$$

$$\because i'_2 = \frac{u_2}{4}, i_2 = \frac{u_2}{2} = 1A \quad \therefore u'_2 = 4V$$

4-18 试用互易定理求题图4-18所示电路中的电流*i*。



解图4-18-1

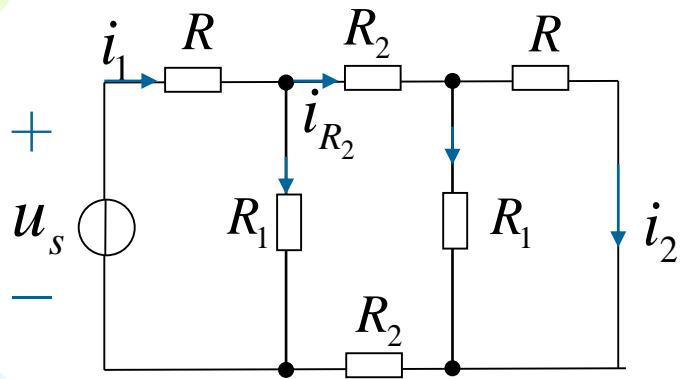


解图4-18-2

$$i_1 = \frac{9}{2 + 3 // 3 + 6 // 3} = \frac{18}{11} \text{ A}$$

$$i = \frac{1}{2} i_1 - \frac{3}{6 + 3} i_1 = \frac{1}{6} i_1 = \frac{3}{11} \text{ A}$$

4-19 在题图4-19电路中，已知 $i_1 = 2A, i_2 = 1A$ ，若把电路中间的 R_2 支路断开，试问此时电流 i_1 为多少？



解一：(1) 断开前：

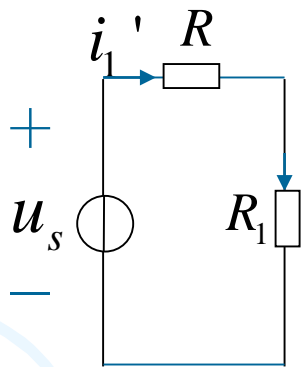
$$i_1 - \frac{u_s - i_1 R}{R_1} = i_{R_2} = i_2 + \frac{i_2 R}{R_1}$$

$$\therefore u_s = R_1 + R$$

(2) 断开后：

$$u_s = i_1' (R_1 + R)$$

$$\therefore i_1' = 1A$$



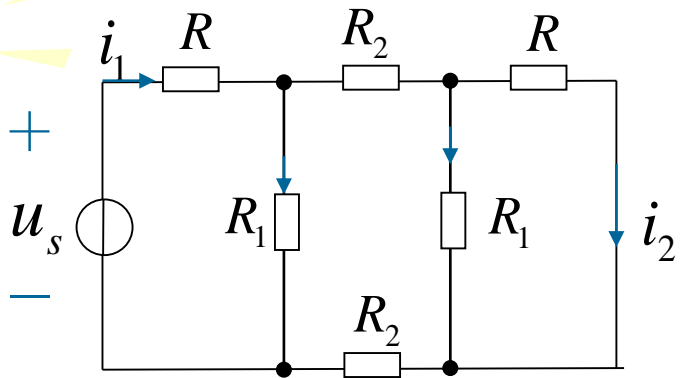


图4-19

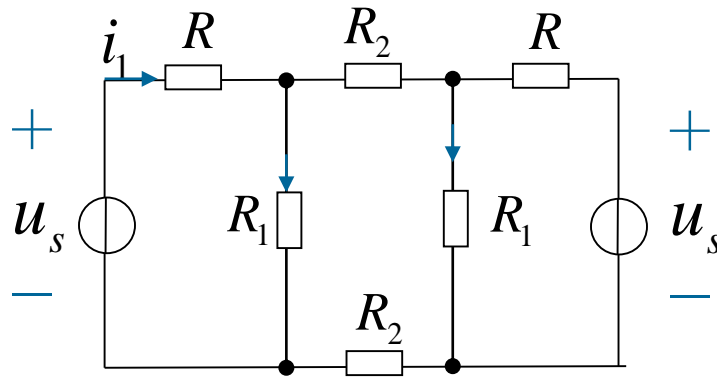


图4-19-1

解二:

求图4-19中 R_2 断开时的电流 i_1 ，相当于求图4-19-1中的电流 i_1 ，而：

$$i_1 = i_1' + i_1''$$

且已知: $i_1' = 2A$

又根据互易定理形式一有:

$$i_1'' = -i_2 = -1A$$

$$\therefore i_1 = i_1' + i_1'' = 1A$$

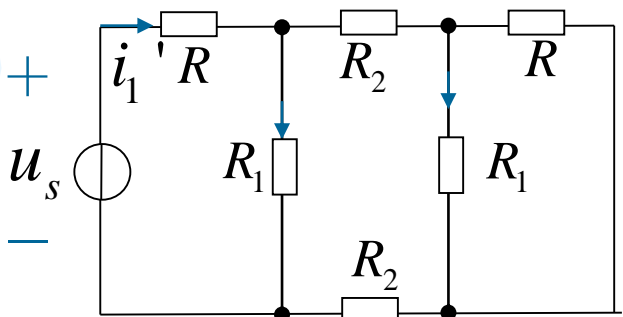


图4-19-2

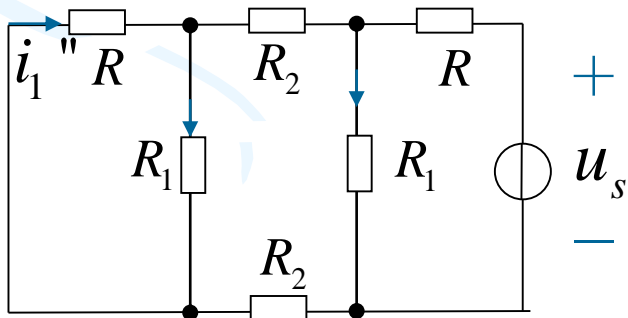
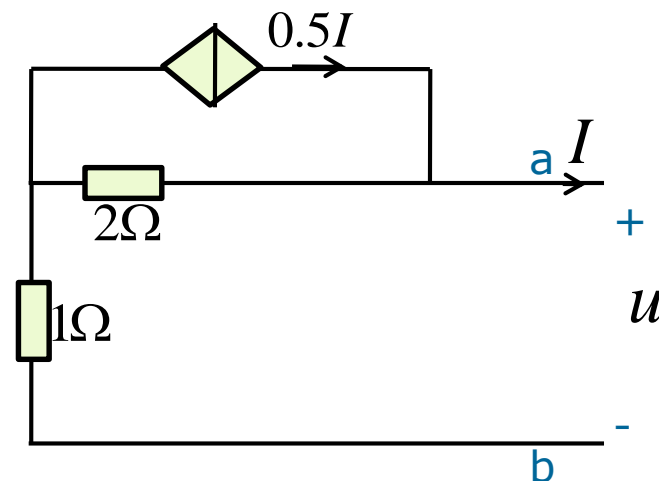
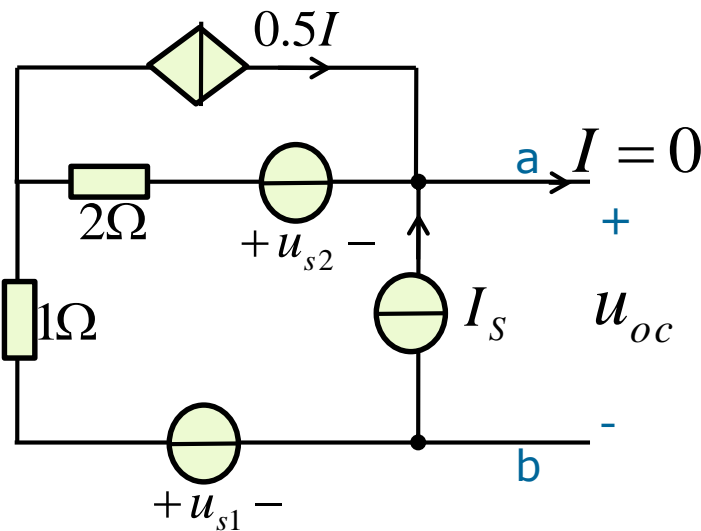
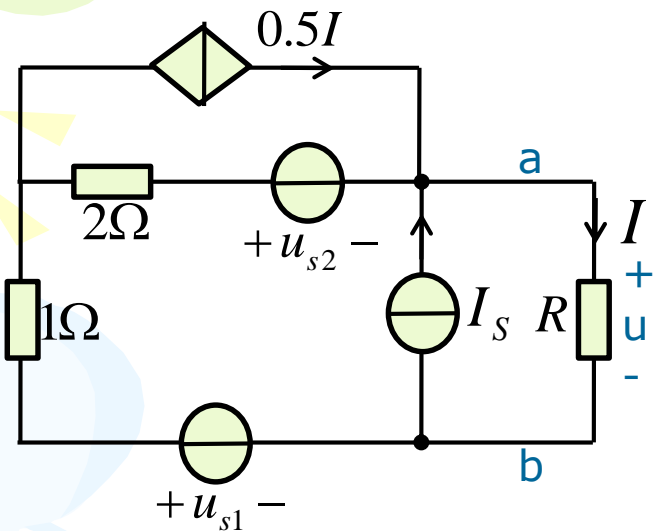


图4-19-3

4-23 已知题图4-23中, 当 $U_{S1} = 1V, R = 1\Omega$ 时, $U = \frac{4}{3}V$,
 试求 $U_{S1} = 1.2V, R = 2\Omega$ 时, $U = ?$



解: 将R左端电路化为戴维南等效电路。

(1) 求开路电压 u_{oc}

因为 $I=0$, 故受控源 $0.5I=0$, 则有:

$$u_{oc} = -U_{S2} + 3I_S + U_{S1}$$

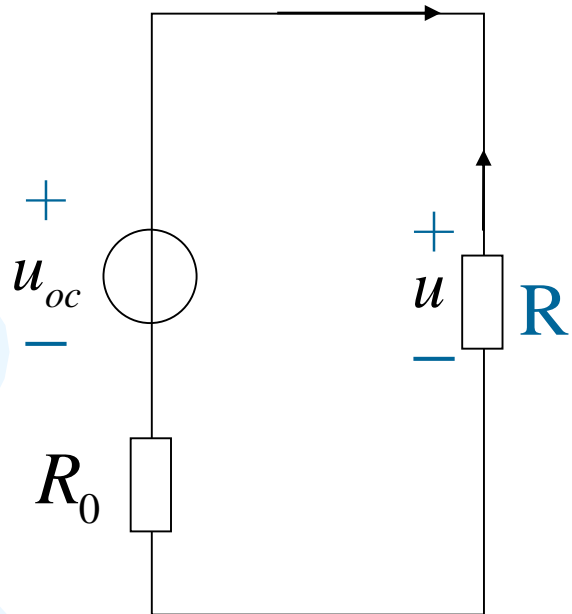
(2) 求输出电阻 R_0

$$u = -2 \times (I - 0.5I) - I = -2I$$

$$R_0 = -\frac{U}{I} = 2\Omega$$

$$\therefore u = \frac{R}{R_0 + R} u_{oc}$$

代入 $R = 1\Omega, U_{S1} = 1V$ 时 $u = \frac{4}{3}V$, 有:



$$u_{oc} = 1 - U_{S2} + 3I_S = \frac{R_0 + R}{R} u$$

$$\therefore -U_{S2} + 3I_S = 3$$

(3) 求当 $U_{S1} = 1.2V, R = 2\Omega$ 时电压 u :

$$\therefore u_{oc} = -U_{S2} + 3I_S + U_{S1}$$

$$\therefore U_{oc} = 4.2V$$

$$U = \frac{2}{2+2} U_{oc} = 2.1V$$

4-23 已知题图4-23中，当 $U_{S1} = 1V, R = 1\Omega$ 时， $u = \frac{4}{3}V$ ，
试求 $U_{S1} = 1.2V, R = 2\Omega$ 时， $u = ?$

另解：

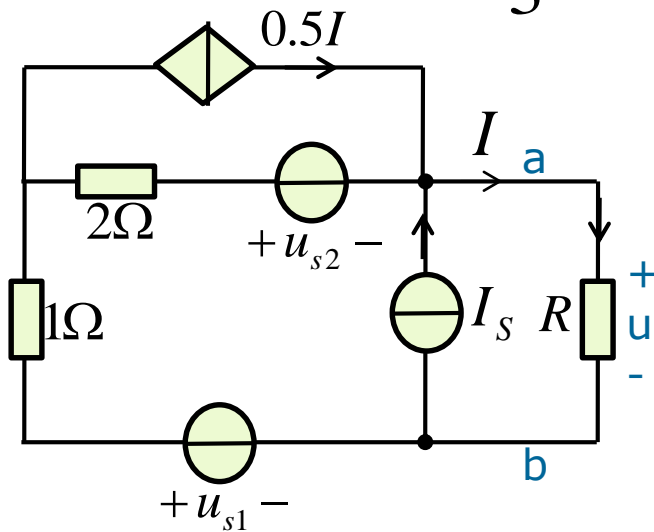
$$u - U_{S1} + 1 \times (I - I_s) + 2 \times (I - 0.5I - I_s) + U_{S2} = 0$$

$$\therefore u - U_{S1} + 2I - 3I_s + U_{S2} = 0 = u - U_{S1} + 2 \cdot \frac{u}{R} - 3I_s + U_{S2}$$

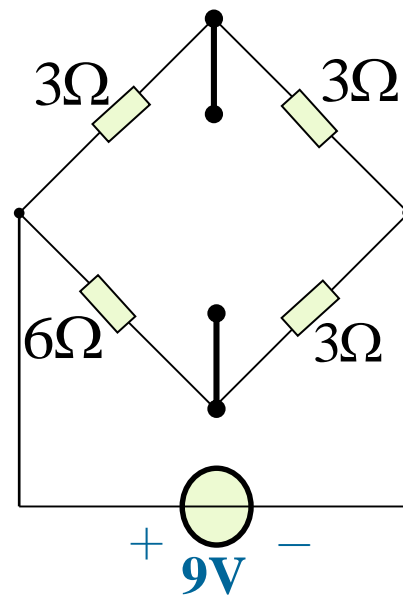
当 $U_{S1} = 1V, R = 1\Omega$ 时，代入 $u = \frac{4}{3}$ ，有：

$$\therefore -U_{S2} + 3I_s = 3$$

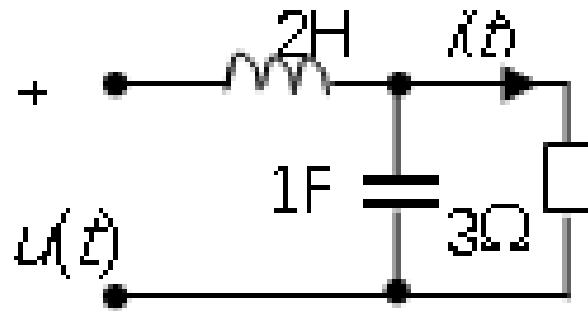
再代入 $U_{S1} = 1.2V, R = 2\Omega$ ，故： $u = 2.1V$



化简。

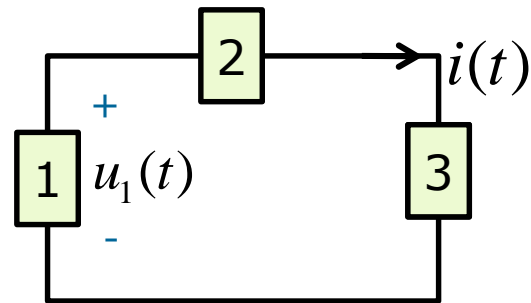


已知 $i(t) = e^{-2t} A$ ， 试求题图6所示电路的。



6-8 已知题图6-8所示电路由一个电阻R、一个电感L和一个电容C组成。且其中 $i(t) = 10e^{-t} - 20e^{-2t} \text{ A}, t \geq 0$, $u_1(t) = -5e^{-t} + 20e^{-2t} \text{ V}, t \geq 0$ 。若在 $t=0$ 时电路总储能为 25J, 试求R、L、C的值。

解: $i_1(t) = i(t) = 10e^{-t} - 20e^{-2t} \text{ A}, t \geq 0$
 $u_1(t) = -5e^{-t} + 20e^{-2t} \text{ V}, t \geq 0$



由于 $u_1(t)$ 和 $\frac{du_1(t)}{dt}$ 与 $i_1(t)$ 的比值不为常数, 故元件**1**肯定不是电阻和电容, 故:

元件1是电感, 且 $L = u_1(t) / \frac{di_1(t)}{dt} = 0.5 \text{ H}$

$$w_L(0) = \frac{1}{2} L i_1^2(0) = \frac{1}{2} \times 0.5 \times (10 - 20)^2 = 25 \text{ J}$$

又因为电路的总储能即：

$$w_C(0) + w_L(0) = 25J$$

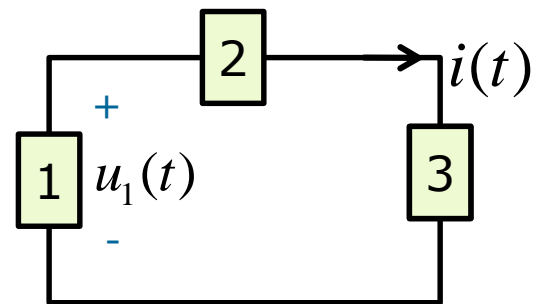
$$\therefore w_C(0) = 0J = \frac{1}{2}Cu_C^2(0)$$

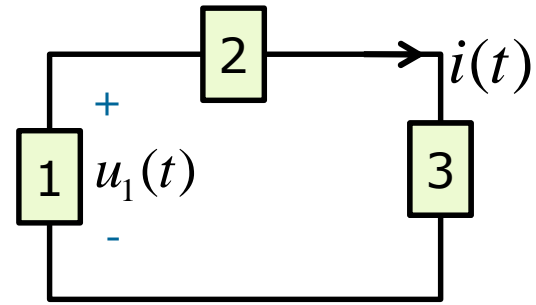
$$\therefore u_C(0) = 0$$

由KVL有： $u_R(0) = -(u_1(0) + u_C(0)) = -15V$

$$\text{而： } u_R(0) = Ri(0) = -10R \quad \therefore R = 1.5\Omega$$

$$\therefore u_R(t) = 1.5i(t) = 15e^{-t} - 30e^{-2t}V$$





$$\therefore u_C(t) = -u_R(t) - u_1(t)$$

$$= -15e^{-t} + 30e^{-2t} - (-5e^{-t} + 20e^{-2t})$$

$$= -10e^{-t} + 10e^{-2t} \text{V}$$

$$i_C(t) = i(t) = 10e^{-t} - 20e^{-2t} \text{A}$$

$$\therefore C = i(t) / \frac{du_C(t)}{dt} = 1 \text{F}$$

直流激励下三要素法求全响应的步骤

1. 计算初始值 $r(0^+)$ (换路前电路已稳定):

(1) 画 $t=0^-$ 图, 求初始状态 $u_C(0^-)$ 或 $i_L(0^-)$;

(2) 由换路定则, 确定 $u_C(0^+)$ 和 $i_L(0^+)$;

(3) 画 $t=0^+$ 图, 求响应初始值 $r(0^+)$: 用数值为 $u_C(0^+)$ 的电压源替代电容或用 $i_L(0^+)$ 的电流源替代电感, 得直流电阻电路再计算 $r(0^+)$;

2. 计算稳态值 $r(\infty)$ (画 $t=\infty$ 图)

根据 $t > 0$ 电路达到新的稳态，将电容用开路或电感用短路代替，得一个直流电阻电路，再对该稳态图进行直流稳态分析确定稳态值 $r(\infty)$

3. 计算时间常数 τ (换路后令所有独立电源置0后的电路图)

先计算与动态元件连接的电阻单口网络的输出电阻 R_o ，然后用 $\tau = R_o C$ 或 $\tau = L/R_o$ 计算时间常数。

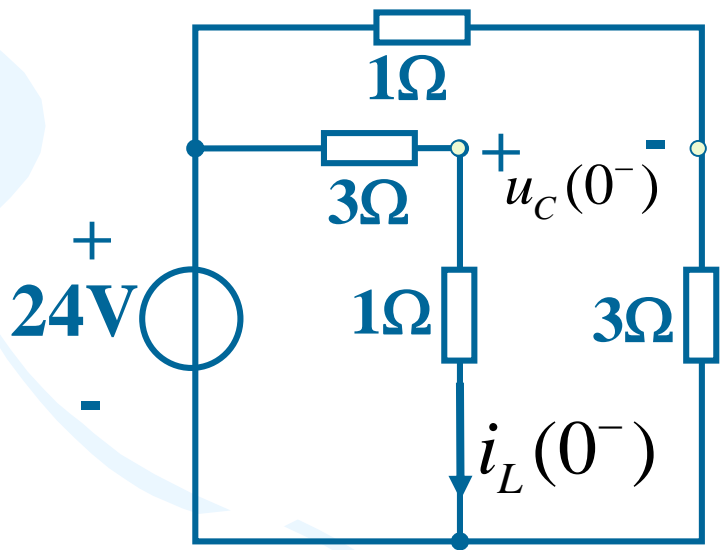


4. 将 $r(0^+)$, $r(\infty)$ 和 τ 代入三要素公式得到**恒定激励**下一阶电路全响应的一般表达式：

$$r(t) = r(\infty) + [r(0^+) - r(\infty)]e^{-t/\tau}, t > 0$$

6-12 题图6-12所示电路原已稳定，开关K在 $t=0$ 时打开，试求 $i_C(0^+)$ 、 $u_1(0^+)$ 和 $\frac{du_C}{dt}\Big|_{t=0^+}$ 。

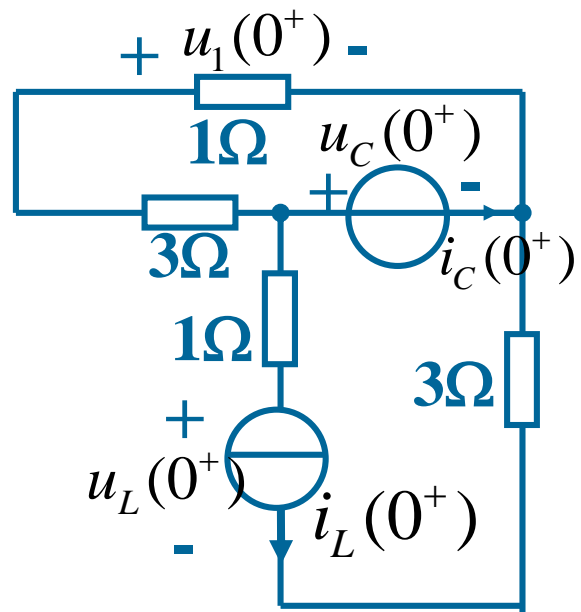
解： $t < 0$ 时电路已稳定，则电容开路，电感短路，有：



$$i_L(0^+) = i_L(0^-) = \frac{24}{1+3} = 6A$$

$$\begin{aligned} u_C(0^+) &= u_C(0^-) \\ &= \frac{1}{1+3} \times 24 - \frac{3}{3+1} \times 24 = -12V \end{aligned}$$

换路后:

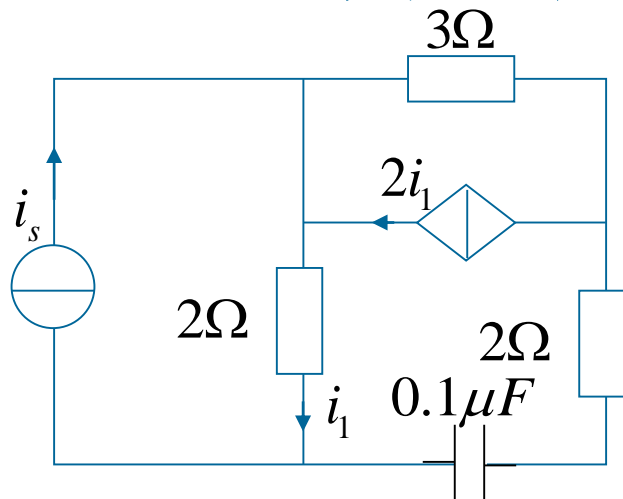


$$u_1(0^+) = \frac{1}{1+3} \times u_C(0^+) = -3V$$

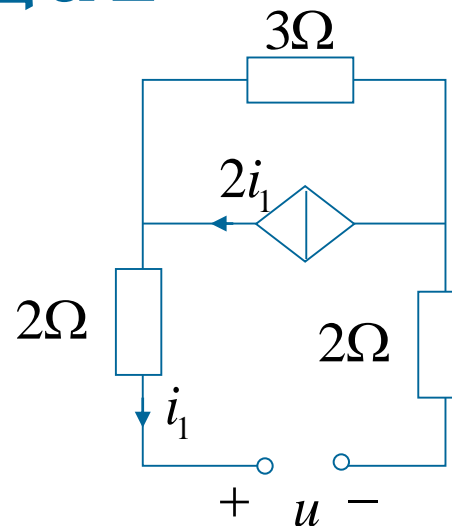
$$i_C(0^+) = -\frac{u_1(0^+)}{1} - i_L(0^+) = -3A$$

$$\left. \frac{du_C}{dt} \right|_{t=0^+} = \frac{1}{C} i_C(0^+) = -6V/s$$

6-14 (d) 等效电阻电路如图d1



(d)



(d1)

$$2i_1 + u + 2i_1 + 3(i_1 - 2i_1) = 0$$

$$u = -i_1$$

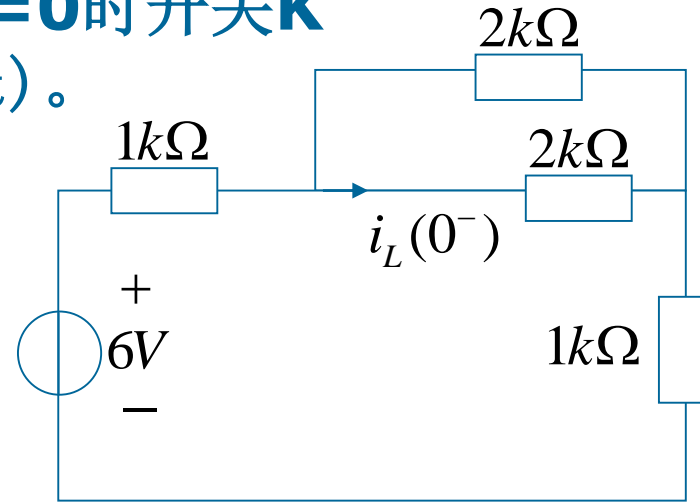
$$R_0 = -\frac{u}{i_1} = 1\Omega$$

$$\tau = R_0 C = 0.1\mu s$$

6-17 题图6-17所示电路原已稳定， $t=0$ 时开关K闭合，试求 $t>0$ 时的 $i_L(t)$ 、 $i(t)$ 和 $i_R(t)$ 。

解：(1)求 $i_L(0^+)$ 、 $i(0^+)$ 和 $i_R(0^+)$ ；

首先求 $i_L(0^-)$ 。换路前电感相当于短路，得 0^- 等效电路如解图(1)，由 0^- 等效电路图得：

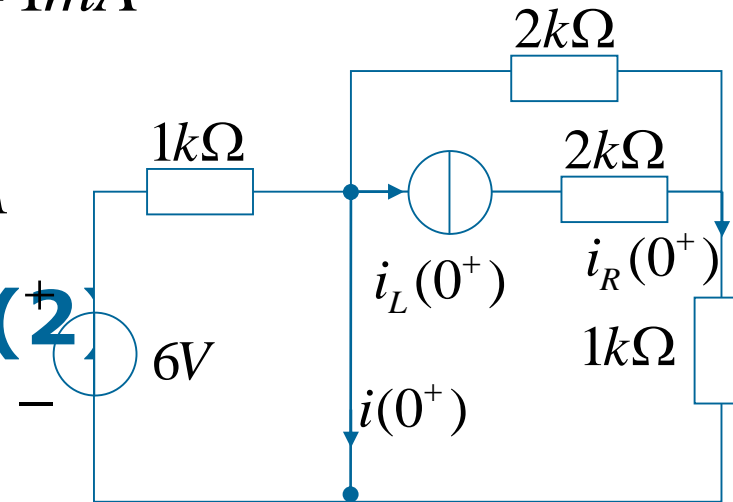


(1) 0^- 图

$$i_L(0^-) = \frac{6}{(1 + 2 // 2 + 1) \times 10^3} \cdot \frac{2}{2 + 2} = 1 \text{mA}$$

由换路定则得 $i_L(0^+) = i_L(0^-) = 1 \text{mA}$

作 0^+ 时刻等效电路如解图5-17(2)



(2) 0^+ 图

$$i_R(0^+) = i_L(0^+) \times \frac{2}{2 + 1} = \frac{2}{3} \text{mA}$$

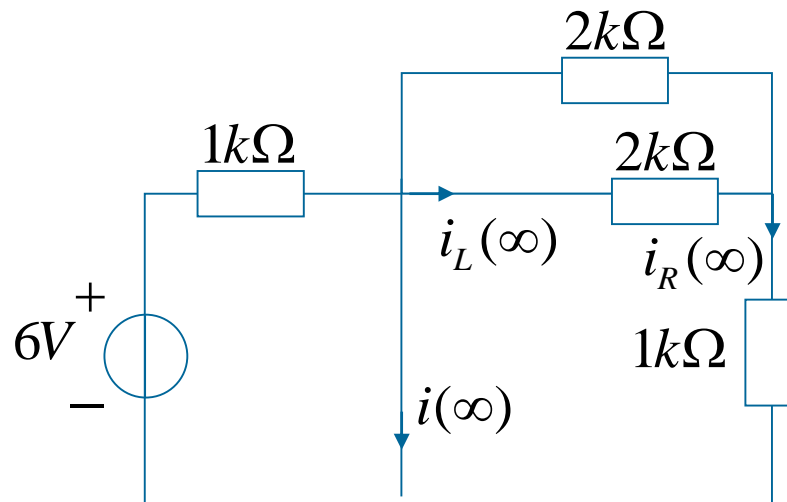
$$i(0^+) = \frac{6}{10^3} - i_R(0^+) = 6 \times 10^{-3} - \frac{2}{3} \times 10^{-3} = \frac{16}{3} \text{mA}$$

(2) 求 $i_L(\infty)$ 、 $i(\infty)$ 和 $i_R(\infty)$

$t \rightarrow \infty$ 时电路达到新的稳定，电感相当于短路，得：

$$i_L(\infty) = 0 \quad i_R(\infty) = 0$$

$$i(\infty) = \frac{6}{10^3} = 6mA$$

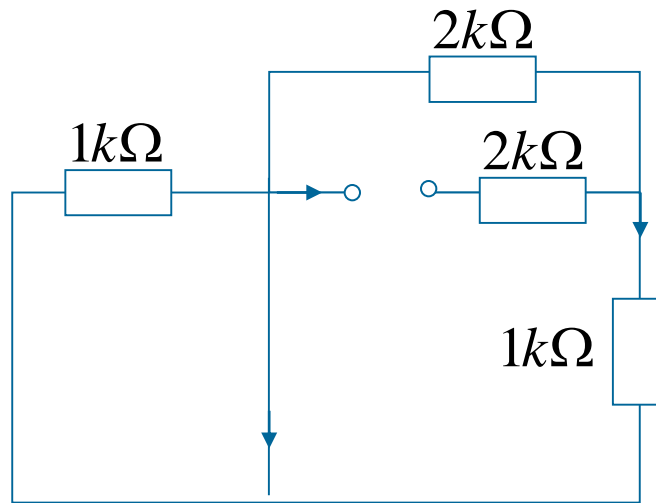


(3) ∞ 图

(3) 求 τ

$$R_{eq} = (2 + 2 // 1) \times 10^3 = \frac{8}{3} \times 10^3 \Omega$$

$$\tau = \frac{L}{R_{eq}} = \frac{3}{4} ms$$



(4) 等效电阻电路

(4) 求 $i_L(t)$, $i(t)$ 和 $i_R(t)$ 由三要素公式:

$$i_L(t) = i_L(\infty) + [i_L(0^+) - i_L(\infty)] e^{-\frac{t}{\tau}} = e^{-\frac{4}{3} \times 10^3 t} \text{ mA}, t \geq 0$$

$$i(t) = i(\infty) + [i(0^+) - i(\infty)] e^{-\frac{t}{\tau}} = 6 - \frac{2}{3} e^{-\frac{4}{3} \times 10^3 t} \text{ mA}, t > 0$$

$$i_R(t) = i_R(\infty) + [i_R(0^+) - i_R(\infty)] e^{-\frac{t}{\tau}} = \frac{2}{3} e^{-\frac{4}{3} \times 10^3 t} \text{ mA}, t > 0$$

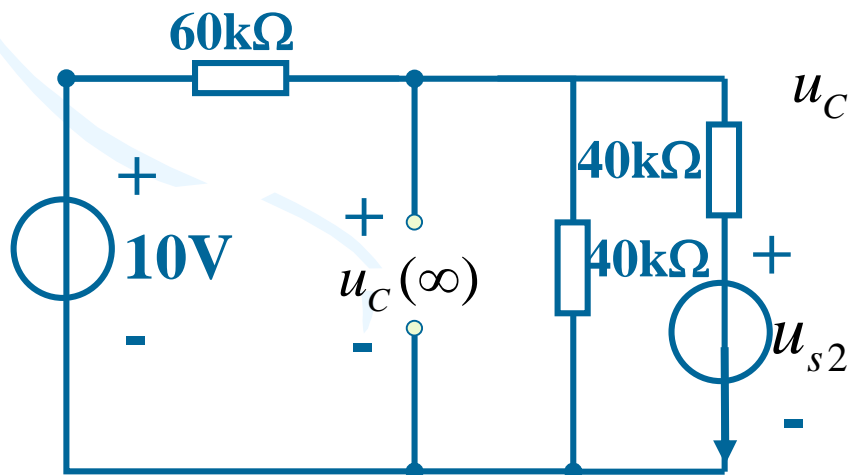
6-26 题图6-26所示电路原已稳定，在 $t=0$ 时开关K闭合。试求(1) $u_{s2} = 6V$ 时的 $u_C(t)$ ， $t > 0$ ；(2) $u_{s2} = ?$ 时，换路后不出现过渡过程。

解：先求 $u_C(t)$ ：

$t < 0$ 时电路已稳定，则电容开路，有：

$$u_C(0^-) = \frac{40}{60 + 40} \times 10 = 4V = u_C(0^+)$$

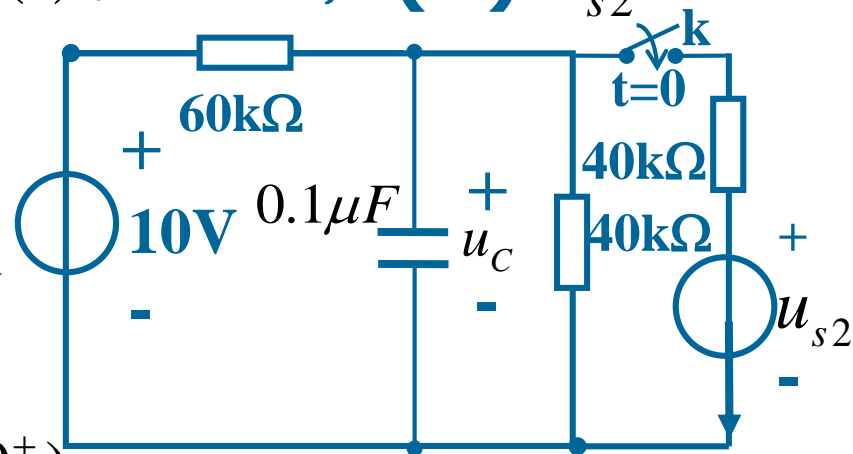
$t \rightarrow \infty$ 时电路已稳定，则电容开路，用叠加法求 $u_C(\infty)$ ：




$$\begin{aligned} u_C(\infty) &= \frac{40 // 40}{40 // 40 + 60} \times 10 + \frac{60 // 40}{60 // 40 + 40} \times u_{s2} \\ &= \frac{10}{4} + \frac{3}{8} u_{s2} \end{aligned}$$

$$R_0 = 40 // 40 // 60 = 15k\Omega$$

$$\therefore \tau = R_0 C = 15 \times 10^3 \times 0.1 \times 10^{-6} = 1.5ms$$




$$\begin{aligned}u_C(t) &= u_C(\infty) + [u_C(0^+) - u_C(\infty)]e^{-\frac{t}{\tau_C}} \\ &= \frac{10}{4} + \frac{3}{8}u_{s2} + \left(4 - \frac{10}{4} - \frac{3}{8}u_{s2}\right)e^{-\frac{2}{3} \times 10^{-3}t}\end{aligned}$$

(1) $u_{s2} = 6V$ 时:

$$\begin{aligned}u_C(t) &= \frac{10}{4} + \frac{3}{8} \times 6 + \left(4 - \frac{10}{4} - \frac{3}{8} \times 6\right)e^{-\frac{2}{3} \times 10^{-3}t} \\ &= 4.75 - 0.75e^{-\frac{2}{3} \times 10^3 t}, t \geq 0\end{aligned}$$

(2) 若要换路后不出现过渡过程, 则:

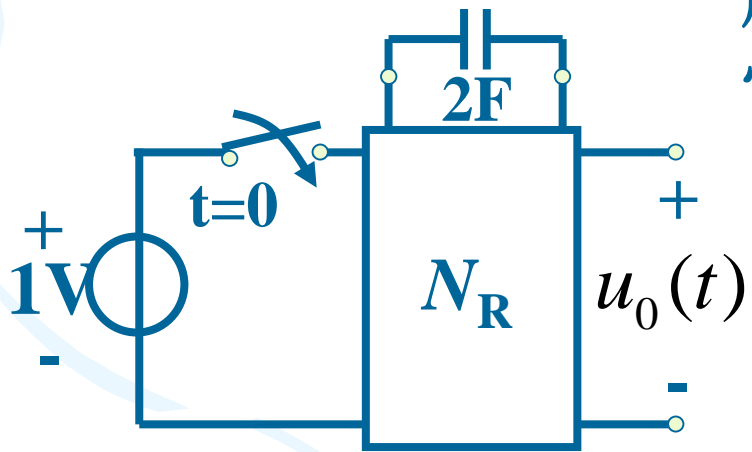
$$4 - \frac{10}{4} - \frac{3}{8}u_{s2} = 0 \quad \therefore u_{s2} = 4V$$

6-30 题图6-30所示电路中， N_R 为线性电阻网络，开关 K 在 $t=0$ 时闭合，已知输出端的零状态响应为

$$u_0(t) = \frac{1}{2} + \frac{1}{8} e^{-0.25t} \text{V}, t > 0$$

若电路中的电容换为 2H 的电感，试求该情况下输出端的零状态响应。

解：是一个直流激励的一阶 RC 线性网络，故应用三要素法：



$$u_{C0}(t) = \frac{1}{2} + \frac{1}{8} e^{-0.25t} \text{V}$$

$$= u_{C0}(\infty) + [u_{C0}(0^+) - u_{C0}(\infty)] e^{-\frac{t}{\tau_C}}$$

故有：

$$u_{C0}(\infty) = \frac{1}{2} \text{V}, u_{C0}(0^+) = u_{C0}(\infty) + \frac{1}{8} = \frac{5}{8} \text{V}$$

$$\tau_C = R_0 C = 4\text{s} \Rightarrow R_0 = 2\Omega$$

应用三要素法求电感电路输出端的零状态响应:

1) 求初始值 $u_{L0}(0^+)$:

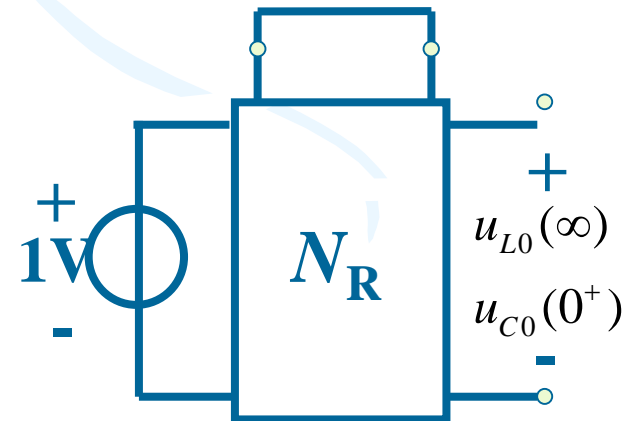
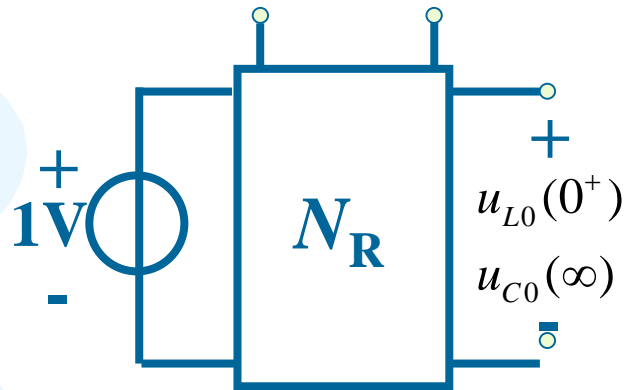
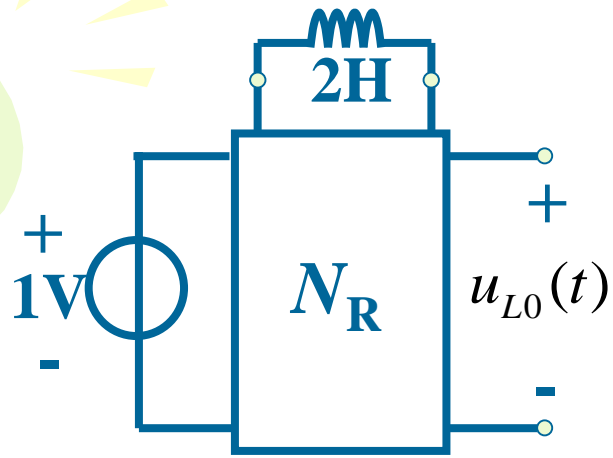
它是 $i_L(0^+) = 0$ 即电感开路时输出端的零状态响应, 与电容电路达到稳态即电容开路时的情况一样, 故:

$$u_{L0}(0^+) = u_{C0}(\infty) = \frac{1}{2} V$$

2) 求稳态值 $u_{L0}(\infty)$:

它是接电感的电路稳态即电感短路时输出端的零状态响应, 与电容电路在 $u_C(0^+) = 0$ 即电容短路时的情况一样, 故:

$$u_{L0}(\infty) = u_{C0}(0^+) = \frac{5}{8} V$$



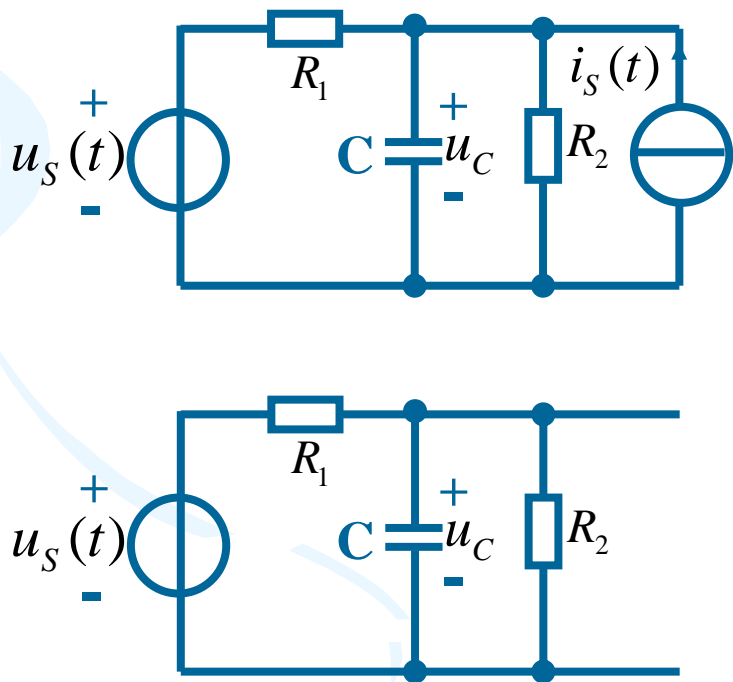
3) 求时间常数 τ_L :

$$\tau_L = \frac{L}{R_0} = 1s$$

4) 写出电感电路的零状态响应:

$$\begin{aligned} u_{L0}(t) &= u_{L0}(\infty) + [u_{L0}(0^+) - u_{L0}(\infty)]e^{-\frac{t}{\tau_L}} \\ &= \frac{5}{8} - \frac{1}{8}e^{-t}V, t > 0 \end{aligned}$$

6-32 题图6-32所示电路中，已知当 $u_S(t) = \varepsilon(t)V, i_S(t) = 0$ 时 $u_C(t) = 2e^{-2t} + \frac{1}{2}V, t > 0$ ；当 $i_S(t) = \varepsilon(t)A, u_S(t) = 0$ 时， $u_C(t) = \frac{1}{2}e^{-2t} + 2V, t > 0$ 。求(1) R_1 、 R_2 和 C ；(2) $u_S(t) = \varepsilon(t)V, i_S(t) = \frac{2}{\varepsilon(t)}A$ 时电路 $u_C(t)$ 的全响应。



解: 1) 当 $u_S(t) = \varepsilon(t)V, i_S(t) = 0$ 时:

$$u_C(t) = 2e^{-2t} + \frac{1}{2}V$$

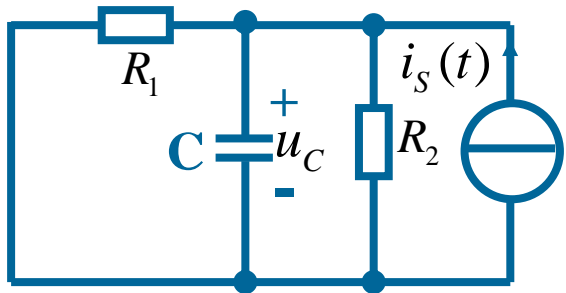
$$= u_C(\infty) + [u_C(0^+) - u_C(\infty)]e^{-\frac{t}{\tau}}$$

$$\therefore u_C(\infty) = \frac{1}{2}, u_C(0^+) = 2 + u_C(\infty) = \frac{5}{2}$$

$$\text{故: } u_{Czi}(t) = \frac{5}{2}e^{-2t}V$$

$$u_{Czs1}(t) = \frac{1}{2}[1 - e^{-2t}]V$$

$$\text{而 } u_C(\infty) = \frac{R_2}{R_1 + R_2} \times 1 = \frac{1}{2} \Rightarrow R_1 = R_2$$



当 $i_s(t) = \varepsilon(t)A, u_s(t) = 0$ 时:

$$u_C(t) = \frac{1}{2}e^{-2t} + 2V, t > 0$$

$$= u_C(\infty) + [u_C(0^+) - u_C(\infty)]e^{-\frac{t}{\tau}}$$

$$\therefore u_C(\infty) = 2, \quad u_C(0^+) = \frac{1}{2} + u_C(\infty) = \frac{5}{2}$$

故: $u_{Czi}(t) = \frac{5}{2}e^{-2t}V, \quad u_{Czs2}(t) = 2[1 - e^{-2t}]V$

而 $u_C(\infty) = \frac{R_1 R_2}{R_1 + R_2} \times 1 = 2$ 且 $R_1 = R_2 \therefore R_1 = R_2 = 4\Omega$

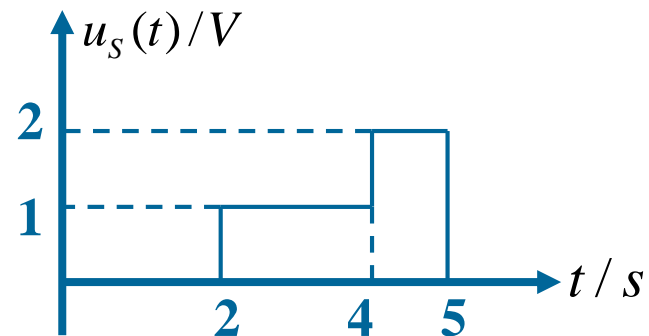
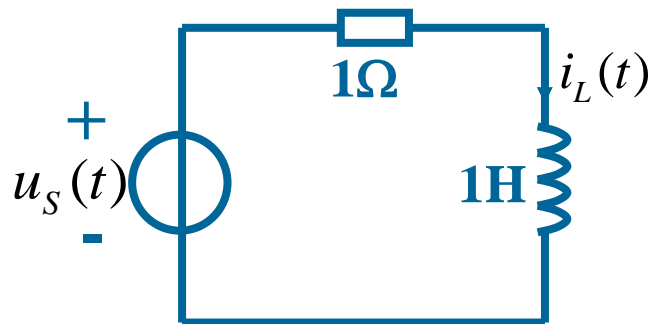
而 $\tau = (R_1 // R_2)C = \frac{1}{2} \Rightarrow C = \frac{1}{4}F$

2) 当 $u_s(t) = \varepsilon(t)V, i_s(t) = \varepsilon(t)A$ 时:

$$u_C(t) = u_{Czi}(t) + u_{Czs1}(t) + u_{Czs2}(t)$$

$$= \frac{5}{2}e^{-2t} + \frac{1}{2}[1 - e^{-2t}] + 2[1 - e^{-2t}] = \frac{5}{2}V, \quad t \geq 0$$

6-33 题图6-33(a)电路中，已知 $i_L(0^-) = 1A$ ，其 $u_S(t)$ 波形如图(b)所示，试求 $i_L(t)$ 。



1) 求零输入响应:

由换路定则可知: $i_L(0^+) = i_L(0^-) = 1A$,

$$\tau = 1s \quad \therefore i_{Lzi}(t) = e^{-t} A, t \geq 0$$

2) 求零状态响应:

当 $u_S(t) = \varepsilon(t)$ 时, $S_{i_L}(\infty) = 1A$; $\therefore S_{i_L}(t) = (1 - e^{-t})\varepsilon(t)$

当 $u_S(t) = \varepsilon(t-2) + \varepsilon(t-4) - 2\varepsilon(t-5)$ 时,

$$\therefore i_{Lzs}(t) = [1 - e^{-(t-2)}]\varepsilon(t-2) + [1 - e^{-(t-4)}]\varepsilon(t-4) - 2[1 - e^{-(t-5)}]\varepsilon(t-5)$$

3) 求全响应:

$$\begin{aligned}\therefore i_L(t) &= i_{Lzi}(t) + i_{Lzs}(t) \\ &= e^{-t} + [1 - e^{-(t-2)}] \varepsilon(t-2) + [1 - e^{-(t-4)}] \varepsilon(t-4) - 2[1 - e^{-(t-5)}] \varepsilon(t-5) A \\ &\quad , t \geq 0\end{aligned}$$