

**8-4** 已知三个同频率的正弦电流： $i_1 = 10 \sin(\omega t + 120^\circ)A$ ， $i_2 = 20 \cos(\omega t - 150^\circ)A$ ， $i_3 = -30 \cos(\omega t - 30^\circ)A$ 。试比较它们的相位差。

解：
$$i_1 = 10 \sin(\omega t + 120^\circ) = 10 \cos(\omega t + 30^\circ)A$$

$$i_2 = 20 \cos(\omega t - 150^\circ)A$$

$$i_3 = -30 \cos(\omega t - 30^\circ) = 30 \cos(\omega t + 150^\circ)A$$

$$\therefore \theta_{12} = 30^\circ - (-150^\circ) = 180^\circ$$

$$\theta_{23} = -150^\circ - 150^\circ = -300^\circ \Rightarrow \theta_{23} = 60^\circ$$

$$\theta_{31} = 150^\circ - 30^\circ = 120^\circ$$

### 8-5 试求下列正弦量的振幅向量和有效值向量:

$$(1)i_1 = 5 \cos \omega t A \quad (2)i_2 = -10 \cos(\omega t + \frac{\pi}{2}) A$$

$$(3)i_3 = 15 \sin(\omega t - 135^\circ) A$$

解: (1) $i_1 = 5 \cos \omega t A \Rightarrow \dot{I}_{1m} = 5 \angle 0^\circ A, I_1 = 2.5\sqrt{2} \angle 0^\circ \approx 3.54 \angle 0^\circ A$

$$(2)i_2 = -10 \cos(\omega t + \frac{\pi}{2}) = 10 \cos(\omega t - \frac{\pi}{2})$$
$$\Rightarrow \dot{I}_{2m} = 10 \angle -\frac{\pi}{2} A, I_2 = 5\sqrt{2} \angle -\frac{\pi}{2} A$$

$$(3)i_3 = 15 \sin(\omega t - 135^\circ) = 15 \cos(\omega t - 225^\circ) = 15 \cos(\omega t + 135^\circ)$$

$$\Rightarrow \dot{I}_{3m} = 15 \angle 135^\circ A, I_3 = 7.5\sqrt{2} \angle 135^\circ A \approx 10.605 \angle 135^\circ A$$

8-6 已知  $\omega = 314 \text{ rad/s}$ ，试写出下列相量所代表的正弦量。

$$(1) \dot{I}_1 = 10 \angle \frac{\pi}{2} \text{ A}$$

$$(2) \dot{I}_{2m} = 2 \angle \frac{3}{4}\pi \text{ A}$$

$$(3) \dot{U}_1 = 3 + j4 \text{ V}$$

$$(4) \dot{U}_{2m} = 5 + j5 \text{ V}$$

$$(1) i_1(t) = 10\sqrt{2} \cos\left(314t + \frac{\pi}{2}\right) \text{ A}$$

$$(2) i_2(t) = 2 \cos\left(314t + \frac{3}{4}\pi\right) \text{ A}$$

$$(3) u_1(t) = 5\sqrt{2} \cos(314t + 53.1^\circ) \text{ V}$$

$$(4) u_2(t) = 5\sqrt{2} \cos(314t + 45^\circ) \text{ V}$$

**8-10** 电路如题图7-10所示, 已知

$$u=100\cos(10t+45^\circ)\text{V}, i_1=i=10\cos(10t+45^\circ)\text{A}$$

$i_2=20\cos(10t+135^\circ)\text{A}$ . 试判断元件**1, 2, 3**的性质及数值。

解: 本题利用**KCL**及元件**VCR**相量形式分析

$$\dot{U}_m = 100\angle 45^\circ\text{V},$$

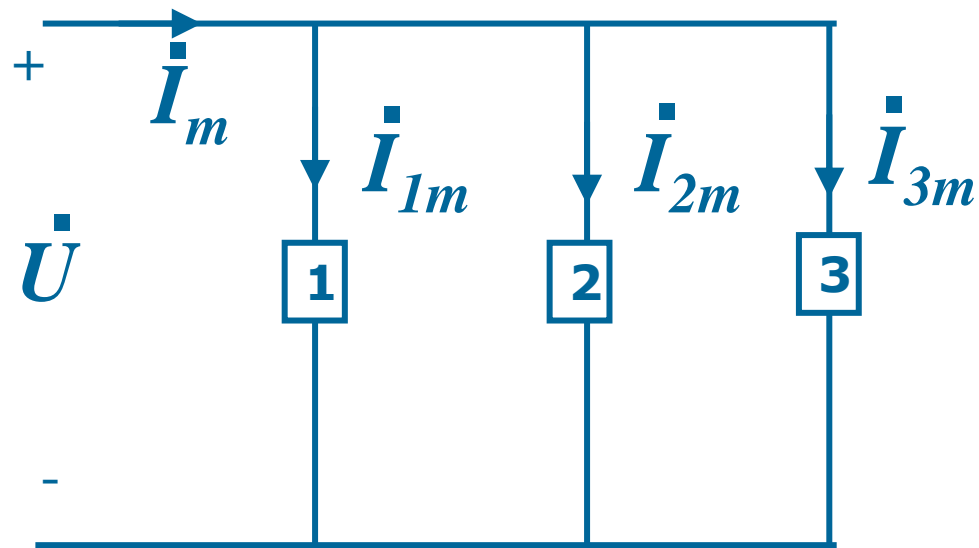
$$\dot{I}_m = \dot{I}_{1m} = 10\angle 45^\circ\text{A},$$

$$\dot{I}_{2m} = 20\angle 135^\circ\text{A}$$

由**KCL**相量形式得

$$\dot{I}_{3m} = \dot{I}_m - \dot{I}_{1m} - \dot{I}_{2m} = 10\angle 45^\circ - 10\angle 45^\circ - 20\angle 135^\circ$$

$$= -20\angle 135^\circ = 20\angle -45^\circ\text{A}$$



对于元件**1**

$$\dot{U}_m = 100 \angle 45^\circ \text{V},$$

$$\dot{I}_{1m} = 10 \angle 45^\circ \text{A},$$

由于其电压电流同相，故  
其为电阻元件，且

$$R = \frac{\dot{U}_m}{\dot{I}_{1m}} = \frac{100 \angle 45^\circ}{10 \angle 45^\circ} = 10 \Omega$$

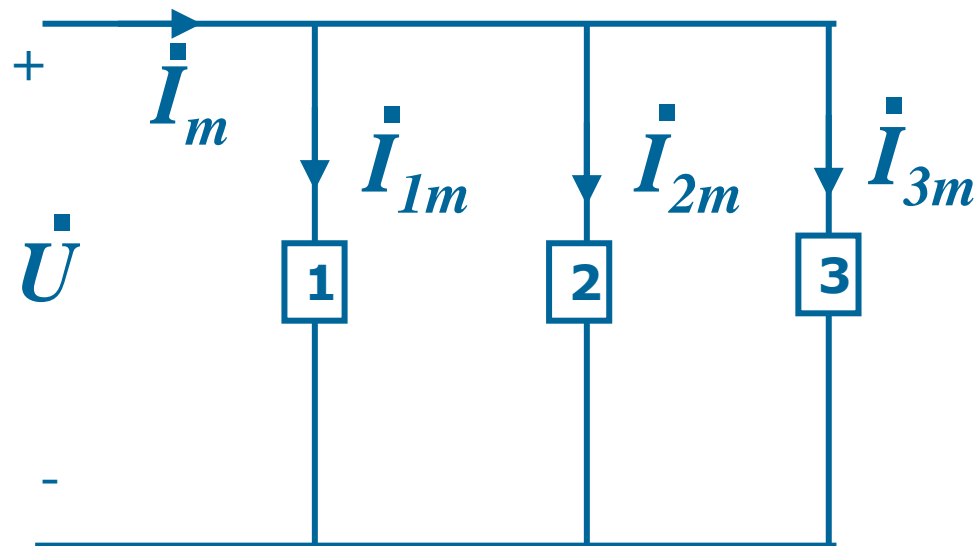
对于元件**2**

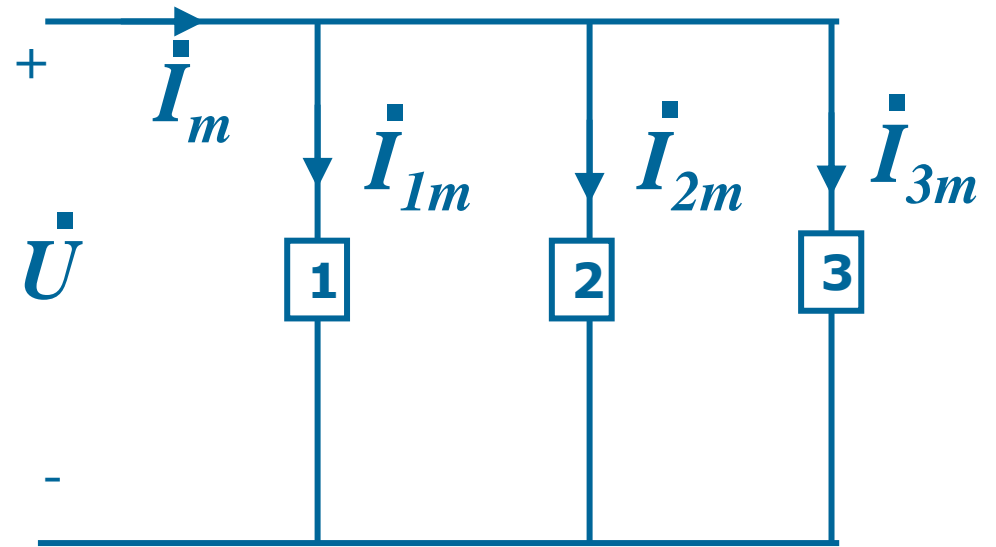
$$\dot{U}_m = 100 \angle 45^\circ \text{V},$$

$$\dot{I}_{2m} = 20 \angle 135^\circ \text{A},$$

由于其电流超前电压**90°**，故  
其为电容元件，且

$$\omega C = \frac{I_m}{U_m} = \frac{20}{100} = \frac{1}{5} \Omega, \quad C = \frac{1}{50} \text{F}$$





对于元件**3**

$$\dot{U}_m = 100 \angle 45^\circ \text{V},$$

$$\dot{I}_{3m} = 20 \angle -45^\circ \text{A},$$

由于其电流滞后电压**90°**，故其为电感元件，且

$$\omega L = \frac{U_m}{I_{3m}} = \frac{100}{20} = 5\Omega, \quad L = 0.5\text{H}$$

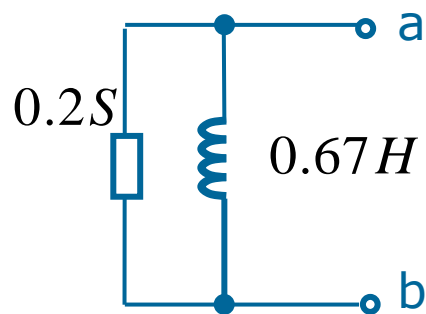
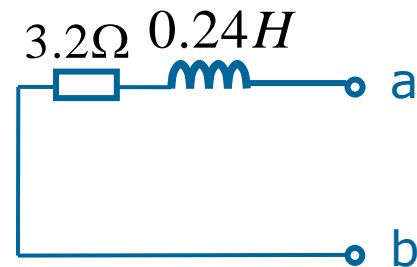
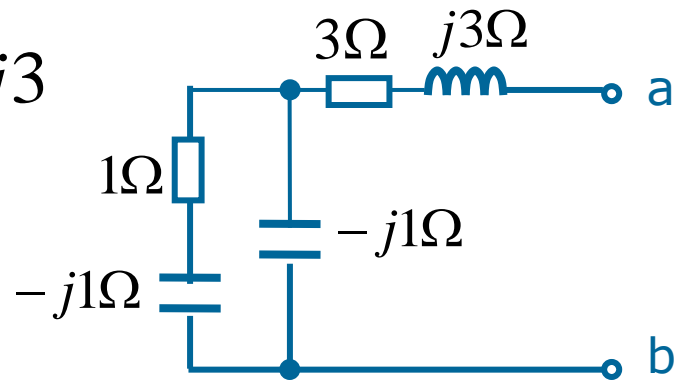
8-13 试求题图7-13所示电路的输入阻抗和导纳，以及该电路的最简串联等效电路和并联等效电路  $\omega = 10 \text{ rad/s}$ 。

解: 
$$Z_{ab} = \frac{(1-j1)(-j1)}{(1-j1) + (-j1)} + 3 + j3$$

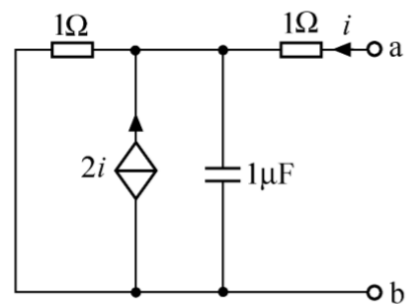
$$= \frac{-1-j1}{1-j2} + 3 + j3$$

$$= \frac{1-j3}{5} + 3 + j3 = 3.2 + j2.4 \Omega$$

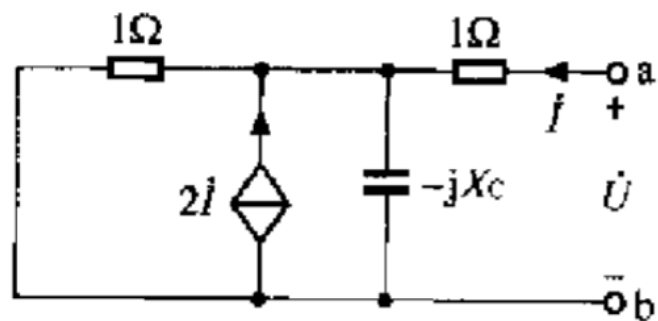
$$Y_{ab} = \frac{1}{Z_{ab}} = \frac{1}{\frac{16}{5} + j\frac{12}{5}} = 0.2 - j0.15 \text{ S}$$



8-15 a 试求题图 8-15 所示各二端网络的输入阻抗。



(a)  $\omega=10^6$  rad/s



作题图 8-15 (a) 的向量模型如解图 8-15 (a) 所示。由于电路中含有受控源，故用加压求流法求其等效阻抗。设在解图 7-15 (a) 端子上加电压  $\dot{U}$ ，此时端子上电流为  $\dot{I}$ ，参考方向如图所示，由 KVL 得

$$\begin{aligned}\dot{U} &= \dot{I} + 1 // (-j1) \times (\dot{I} + 2\dot{I}) \\ &= \dot{I} + \frac{-j1}{1-j1} \times 3\dot{I} = \frac{1-j4}{1-j1}\dot{I}\end{aligned}$$

故

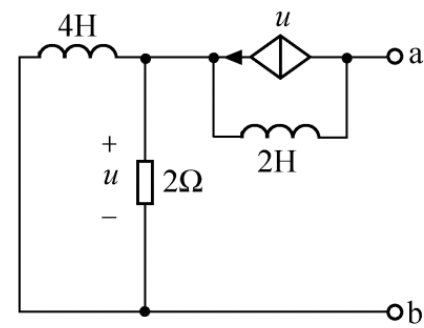
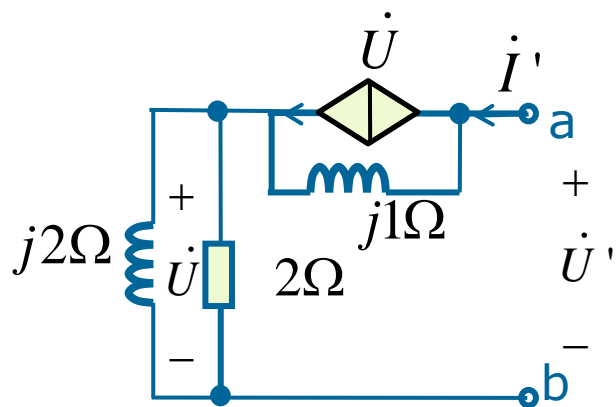
$$Z_{in} = \frac{\dot{U}}{\dot{I}} = \frac{1-j4}{1-j1} = \frac{5}{2} - j\frac{3}{2}\Omega$$



8-15b

试求题图7-15所示各二端网络的输入阻抗。

解:



(b)  $\omega=0.5\text{rad/s}$

$$\dot{U}' = j\dot{I}' - j\dot{U} + \dot{U}$$

$$\dot{U} = \dot{I}'(2 // j2)$$

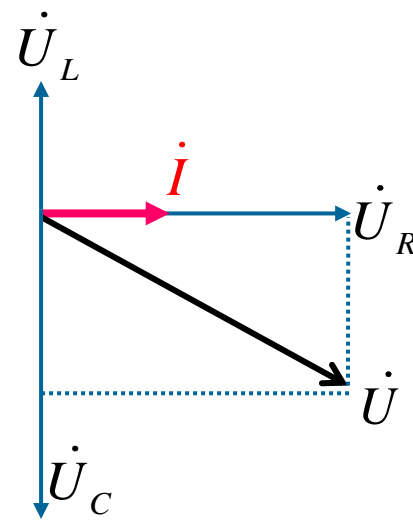
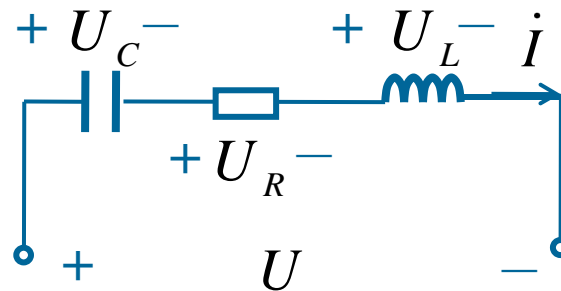
$$\therefore \dot{U}' = j\dot{I}' + \frac{j4}{2 + j2}(1 - j)\dot{I}' = (2 + j1)\dot{I}'$$

$$\therefore Z_i = (2 + j1)\Omega$$

8-16 在题图7-16所示电路中, 已知  $U_C = 15V, U_L = 12V,$   
 $U_R = 4V,$  求电压  $U$  为多少?

解: 
$$U = \sqrt{U_R^2 + (U_L - U_C)^2}$$

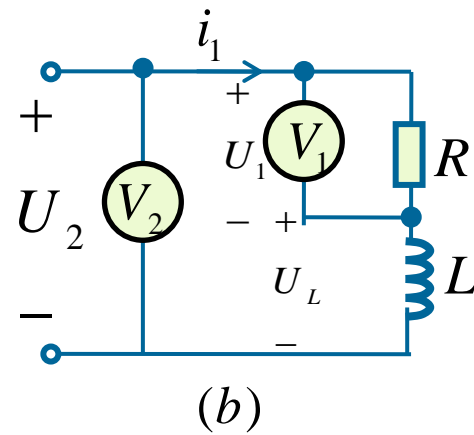
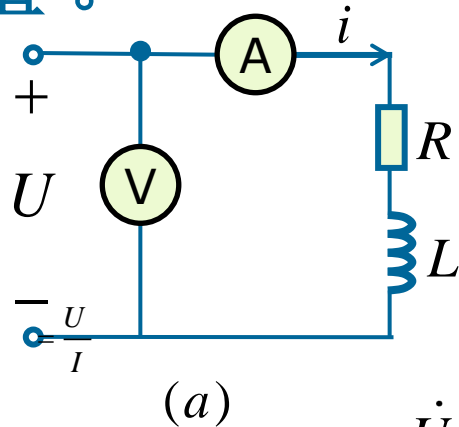
$$= \sqrt{4^2 + (12 - 15)^2} = 5V$$



**8-18** RL串联电路，在题图7-18(a)直流情况下，电流表的读数为50mA，电压表的读数为6V。在  $f = 10^3 \text{ Hz}$  交流情况下，电压表  $V_1$  读数为6V， $V_2$  读数为10V，如图(b)所示。试求R、L的值。

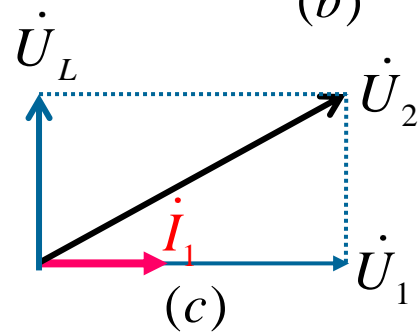
解：直流时电感相当于短路，则：

$$R = \frac{U}{I} = \frac{6}{50 \times 10^{-3}} = 120 \Omega$$



交流时相量图如图(c)，则：

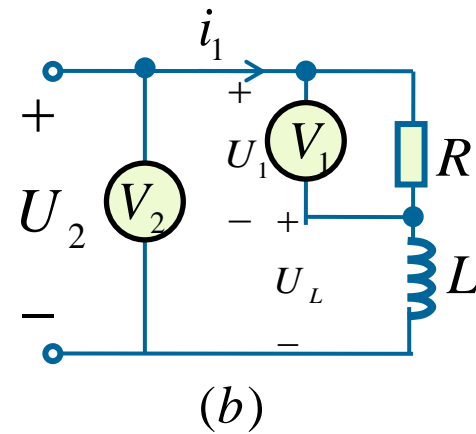
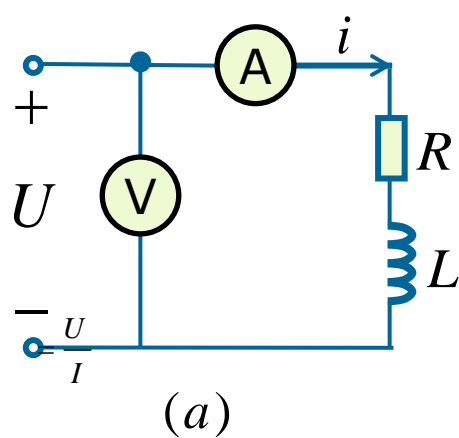
$$U_L = \sqrt{U_2^2 - U_1^2} = 8 \text{ V}$$



$$\therefore \frac{U_1}{R} = \frac{U_L}{\omega L} \quad \therefore L = \frac{U_L R}{\omega U_1} = \frac{8 \times 120}{2\pi \times 10^3 \times 6} = 25.5 \text{ mH}$$

另解：直流时电感相当于短路，则：

$$R = \frac{U}{I} = \frac{6}{50 \times 10^{-3}} = 120 \Omega$$

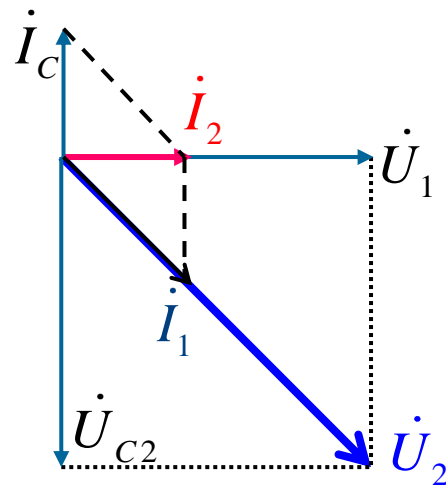
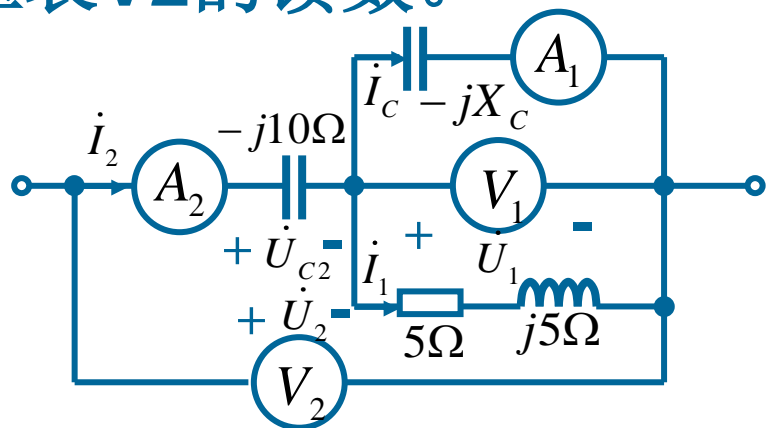


交流时设  $\dot{U}_1 = 6 \angle 0^\circ \text{V}$ ，则：
$$\dot{I}_1 = \frac{\dot{U}_1}{R} = \frac{6 \angle 0^\circ}{120} = 0.05 \angle 0^\circ \text{A}$$

$$\because Z = R + j\omega L \quad \therefore |Z| = \sqrt{R^2 + (\omega L)^2} = \frac{U_2}{I_1} = 200$$

$$\therefore L = \frac{\sqrt{200^2 - R^2}}{\omega} = 25.5 \text{mH}$$

**8-19** 题图7-19所示电路，已知电流表A1的读数为10A，电压表V1的读数为100V；试画相量图求电流表A2和电压表V2的读数。



解：设各电压、电流如图，且设  $\dot{U}_1$  为参考向量，则：

$$\dot{U}_1 = 100 \angle 0^\circ \quad \therefore \dot{I}_C = \frac{\dot{U}_1}{-jX_C} = \frac{U_1 \angle 0^\circ}{X_C \angle -90^\circ} = 10 \angle 90^\circ \text{ A}$$

$$\dot{I}_1 = \frac{\dot{U}_1}{5 + j5} = \frac{100 \angle 0^\circ}{5\sqrt{2} \angle 45^\circ} = 10\sqrt{2} \angle -45^\circ \text{ A}$$

故由相量图可得：  $\therefore \dot{I}_2 = \dot{I}_1 + \dot{I}_C = 10 \angle 0^\circ \text{ A}$  由相量图：

$$\dot{U}_{C2} = (-j10)\dot{I}_2 = 100 \angle -90^\circ \text{ V} \quad \dot{U}_2 = \dot{U}_{C2} + \dot{U}_1 = 100\sqrt{2} \angle -45^\circ$$

8-22(b) 试分别列写下列电路的网孔方程和节点方程，各图中  $u_s = 10 \cos 2tV$ ， $i_s = 0.5 \cos(2t - 30^\circ)A$ 。

解：(1) 列网孔方程：

有效值相量：

$$\dot{I}_s = \frac{0.5 \angle -30^\circ}{\sqrt{2}} A$$

$$\dot{U}_s = \frac{10 \angle 0^\circ}{\sqrt{2}} V$$

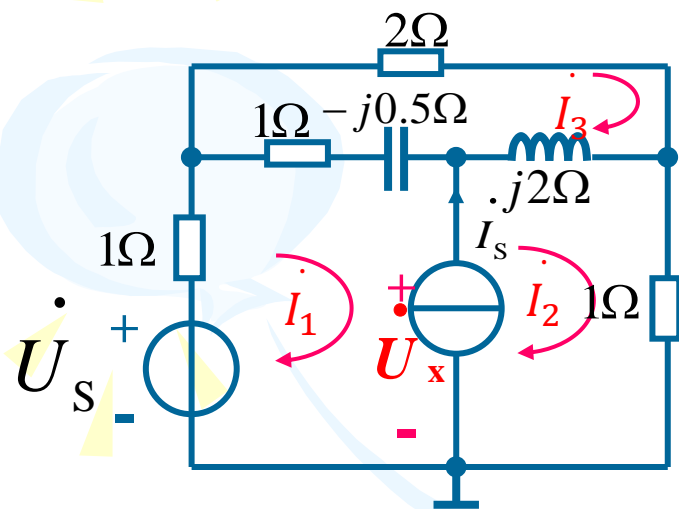
$$(2 - j0.5) \dot{I}_1 - (2 - j0.5) \dot{I}_3 = \frac{10 \angle 0^\circ}{\sqrt{2}} - \dot{U}_x$$

$$(1 + j2) \dot{I}_2 - j2 \dot{I}_3 = \dot{U}_x$$

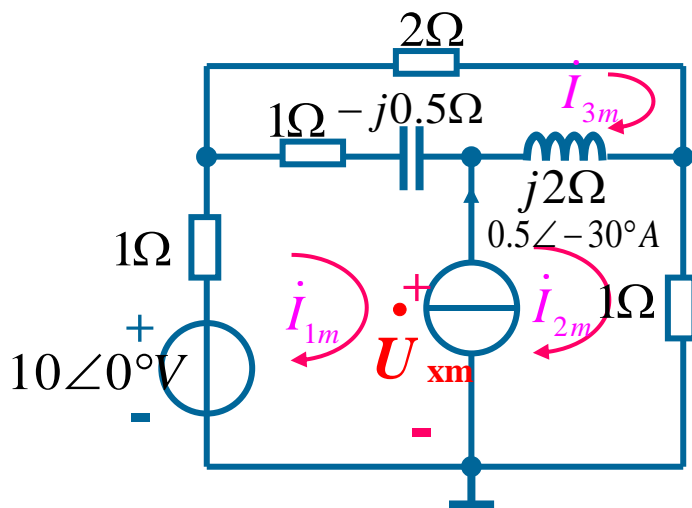
$$-(1 - j0.5) \dot{I}_1 - j2 \dot{I}_2 + (3 + j1.5) \dot{I}_3 = 0$$

$$\dot{I}_2 - \dot{I}_1 = \frac{0.5 \angle -30^\circ}{\sqrt{2}}$$

振幅相量和有效值相量都有，推荐有效值相量做！



振幅相量:



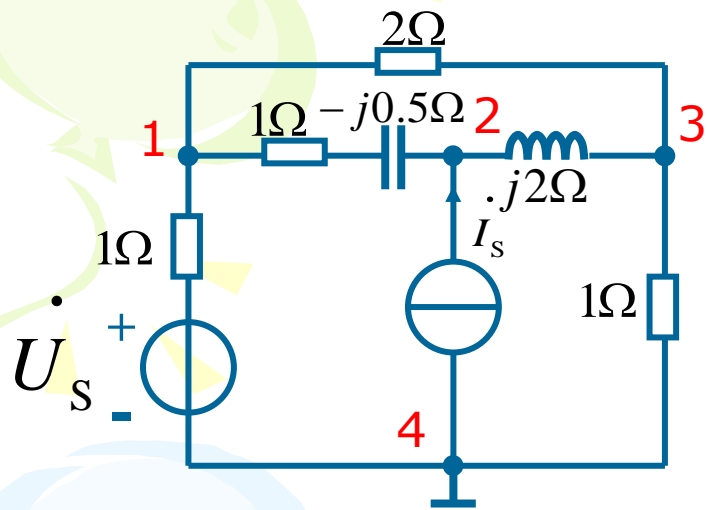
$$\dot{I}_{Sm} = 0.5 \angle -30^\circ \text{ A}$$

$$\dot{U}_{Sm} = 10 \angle 0^\circ \text{ V}$$

$$\begin{cases} (2 - j0.5) \dot{I}_{1m} - (2 - j0.5) \dot{I}_{3m} = 10 \angle 0^\circ - \dot{U}_{xm} \\ (1 + j2) \dot{I}_{2m} - j2 \dot{I}_{3m} = \dot{U}_{xm} \\ -(1 - j0.5) \dot{I}_{1m} - j2 \dot{I}_{2m} + (3 + j1.5) \dot{I}_{3m} = 0 \\ \dot{I}_{2m} - \dot{I}_{1m} = 0.5 \angle -30^\circ \end{cases}$$

## (2) 列节点方程:

有效值相量:



$$\dot{I}_S = \frac{0.5 \angle -30^\circ}{\sqrt{2}} \text{ A}$$
$$\dot{U}_S = \frac{10 \angle 0^\circ}{\sqrt{2}} \text{ V}$$

$$\left(1 + \frac{1}{2} + \frac{1}{1-0.5j}\right) \dot{U}_1 - \frac{1}{1-0.5j} \dot{U}_2 - \frac{1}{2} \dot{U}_3 = \frac{10 \angle 0^\circ}{\sqrt{2}}$$

$$-\frac{1}{1-0.5j} \dot{U}_1 + \left(\frac{1}{2j} + \frac{1}{1-0.5j}\right) \dot{U}_2 - \frac{1}{2j} \dot{U}_3 = \frac{0.5 \angle -30^\circ}{\sqrt{2}}$$

$$-\frac{1}{2} \dot{U}_1 - \frac{1}{2j} \dot{U}_2 + \left(\frac{1}{2} + 1 + \frac{1}{2j}\right) \dot{U}_3 = 0$$

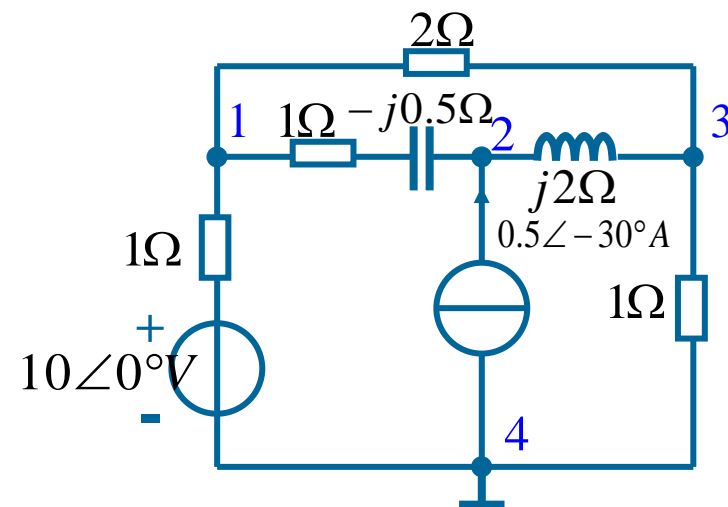
注:  $1-0.5j$  是一条支路, 作为一个整体, 是一个阻抗



振幅相量:

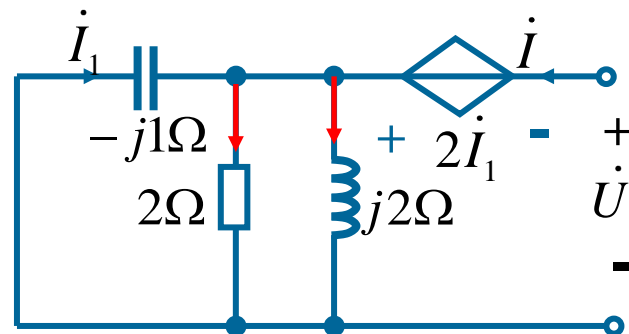
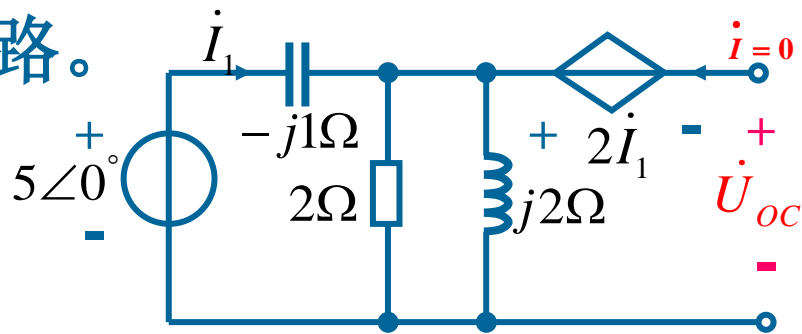
$$\dot{I}_{S_m} = 0.5 \angle -30^\circ \text{ A}$$

$$\dot{U}_{S_m} = 10 \angle 0^\circ \text{ V}$$



$$\begin{cases} \left(1 + \frac{1}{2} + \frac{1}{1-0.5j}\right) \dot{U}_{1m} - \frac{1}{1-0.5j} \dot{U}_{2m} - \frac{1}{2} \dot{U}_{3m} = \frac{10 \angle 0^\circ}{1} \\ -\frac{1}{1-0.5j} \dot{U}_{1m} + \left(\frac{1}{2j} + \frac{1}{1-0.5j}\right) \dot{U}_{2m} - \frac{1}{2j} \dot{U}_{3m} = 0.5 \angle -30^\circ \\ -\frac{1}{2} \dot{U}_{1m} - \frac{1}{2j} \dot{U}_{2m} + \left(\frac{3}{2} + \frac{1}{2j}\right) \dot{U}_{3m} = 0 \end{cases}$$

8-23(b) 试求题图7-23所示有源二端网络的戴维南等效电路。



解: (1) 求开路电压  $\dot{U}_{oc}$  :

$$\begin{cases} \dot{U}_{oc} = -2\dot{I}_1 - (-j1)\dot{I}_1 + 5\angle 0^\circ \\ \dot{I}_1 = \frac{5\angle 0^\circ}{-j1 + (2 // j2)} = 5\angle 0^\circ \end{cases}$$

$$\therefore \dot{U}_{oc} = -5 + j5 = 5\sqrt{2}\angle 135^\circ$$

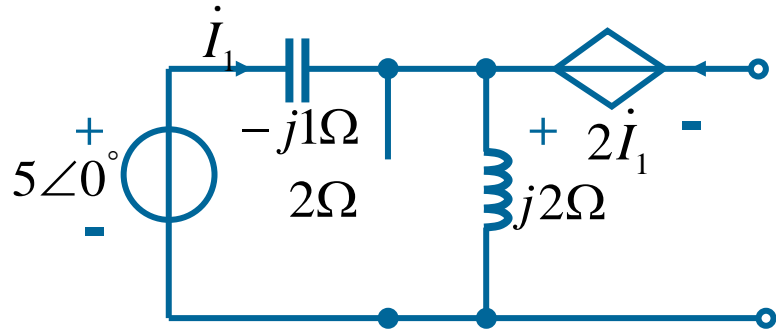
(2) 求等效阻抗  $Z_0$  :

$$\begin{cases} \dot{U} = -2\dot{I}_1 - (-j\dot{I}_1) \\ \dot{I} = -\dot{I}_1 + \frac{(-j1)(-\dot{I}_1)}{2} + \frac{(-j1)(-\dot{I}_1)}{j2} \end{cases}$$

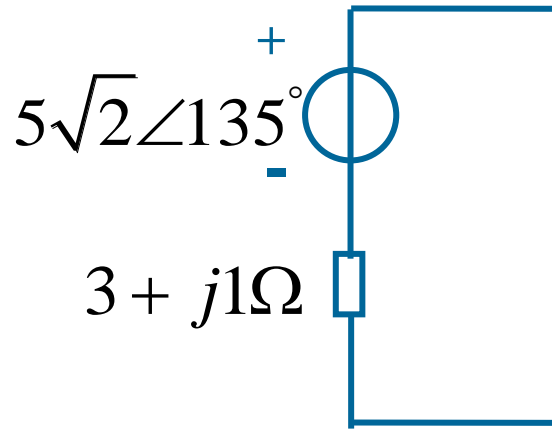
$$\text{或: } \begin{cases} \dot{U} = -2\dot{I}_1 - (-j\dot{I}_1) \\ \dot{I}_1 = -\frac{\frac{1}{-j1}}{\frac{1}{-j1} + \frac{1}{2} + \frac{1}{j2}} \dot{I} \text{ (分流公式)} \end{cases}$$

$$\text{可得: } \dot{U} = (3 + j1)\dot{I}$$

$$\therefore Z_0 = (3 + j1)\Omega$$



戴维南等效电路图:



说明: 若给的图是时域的, 则等效戴维南电路图也必须是时域的, 即: 要将  $Z_0 = (3 + j1)$  转换成一电阻串联电感。

8-25 (2) 已知关联参考方向下的无源二端网络的端口电压  $u(t)$  和电流  $i(t)$  分别为  $u(t) = 10 \cos(100t + 70^\circ) \text{V}$  和  $i(t) = 2 \cos(100t + 40^\circ) \text{A}$ , 试求各种情况下的  $P$ 、 $Q$  和  $S$ 。

解: 先将各量写成相量形式:

$$\dot{U} = 5\sqrt{2} \angle 70^\circ \text{V}, \quad \dot{i} = \sqrt{2} \angle 40^\circ \text{A}$$

$$P = UI \cos \theta_z = 5\sqrt{2} \times \sqrt{2} \cos 30^\circ = 5\sqrt{3} \text{W}$$

$$Q = UI \sin \theta_z = 5\sqrt{2} \times \sqrt{2} \sin 30^\circ = 5 \text{Var}$$

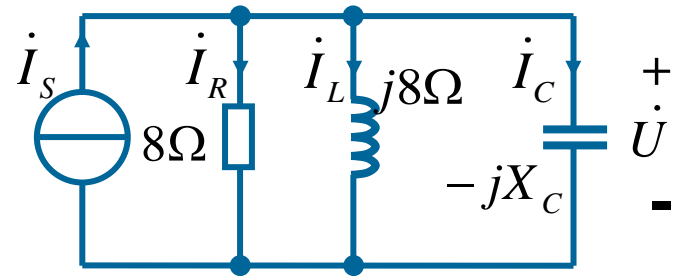
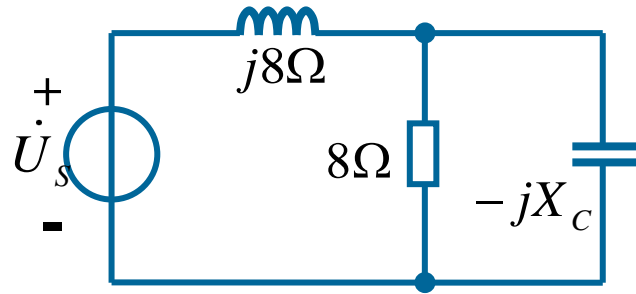
$$S = UI = 10 \text{VA}$$

另解:  $\tilde{S} = \dot{U} \dot{I}^* = 5\sqrt{2} \angle 70^\circ \times \sqrt{2} \angle -40^\circ$

$$= 10 \angle 30^\circ = 5\sqrt{3} + j5$$

$$\therefore P = 5\sqrt{3} \text{W}, \quad Q = 5 \text{Var}, \quad S = 10 \text{VA}$$

**8-27** 二端网络如题图7-27所示，已知  $\dot{U}_S = 50\angle 0^\circ \text{V}$ ，电源提供的平均功率为  $312.5\text{W}$ ，试求  $X_C$  的数值。



解：将电路等效为诺顿模型，并设各支路电流和电压如相量模型图所示，其中：

$$\dot{I}_S = \frac{\dot{U}_S}{j8} = 6.25\angle -90^\circ \text{A}$$

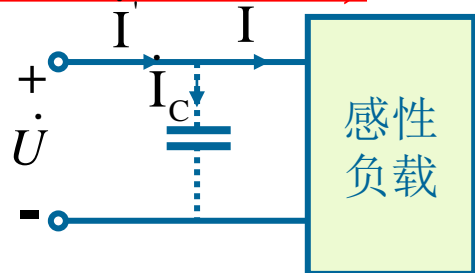
$$P = I_R^2 R = 312.5 \Rightarrow I_R = 6.25 \text{A}$$

$$\because \dot{I}_S = \dot{I}_R + \dot{I}_C + \dot{I}_L \quad \text{即} \quad I_S = \sqrt{(I_C - I_L)^2 + I_R^2} \quad \text{且} \quad \because I_R = I_S$$

$$\therefore I_C = I_L \quad \text{而} \quad I_C = \frac{U}{X_C}, I_L = \frac{U}{8} \quad \therefore X_C = 8\Omega$$

**8-28** 如题图7-28所示, 已知某感性负载接于电压220V、频率50Hz的交流电源上, 其吸收的平均功率为40W, 端口电流 $I=0.66\text{A}$ , 试求感性负载的功率因数; 如欲使电路的功率因数提高到0.9, 问至少需并联多大电容 $C$ ?

**(213页例题8-20)**



解:  $\because P = UI \cos \theta_Z$

$$\text{故: } p_f = \cos \theta_Z = \frac{P}{UI} = \frac{40}{220 \times 0.66} \approx 0.275$$

$$\text{且 } \theta_Z = 74^\circ$$

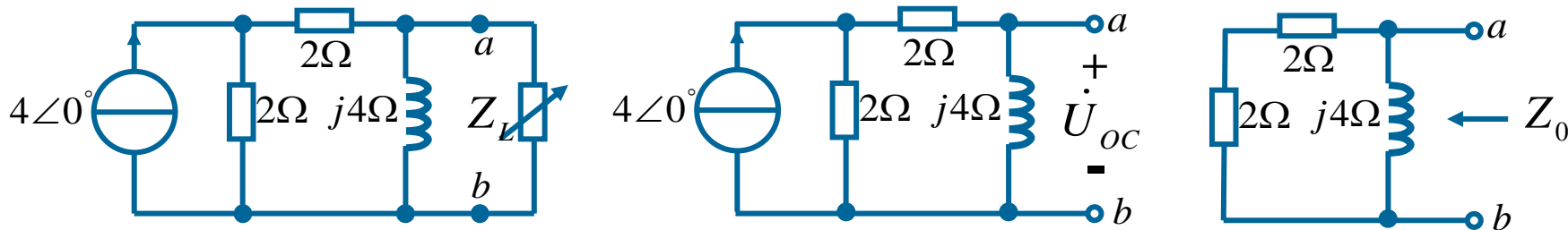
$$\text{当 } p'_f = \cos \theta'_Z = 0.9, \quad I' = \frac{P}{U \cdot p'_f} = \frac{40}{220 \times 0.9} \approx 0.202\text{A}$$

$$\text{且 } \theta_Z = 25.8^\circ \quad \text{设 } \dot{U} = 220 \angle 0^\circ$$

$$\therefore \dot{I}_C = \dot{I}' - \dot{I} = 0.202 \angle -25.8^\circ - 0.66 \angle -74^\circ \approx j0.55\text{A}$$

$$\because I_C = \omega C U \Rightarrow C = \frac{I_C}{2\pi f U} = \frac{0.55}{2 \times 3.14 \times 50 \times 220} \approx 7.9 \mu\text{f}$$

8-29 正弦稳态电路如题图7-29所示，若 $Z_L$ 可变，试问为何值时可获得最大功率？最大功率 $P_{\max}$ 为多少？



解：1) 求开路电压  $\dot{U}_{oc}$ ：

$$\dot{U}_{oc} = 4\angle 0^\circ \times \frac{2}{2+2+j4} \times j4 = \frac{8\angle 90^\circ}{\sqrt{2}\angle 45^\circ} = 4\sqrt{2}\angle 45^\circ \text{ V}$$

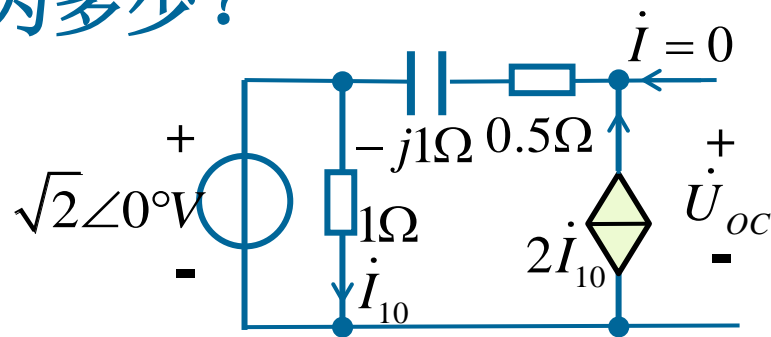
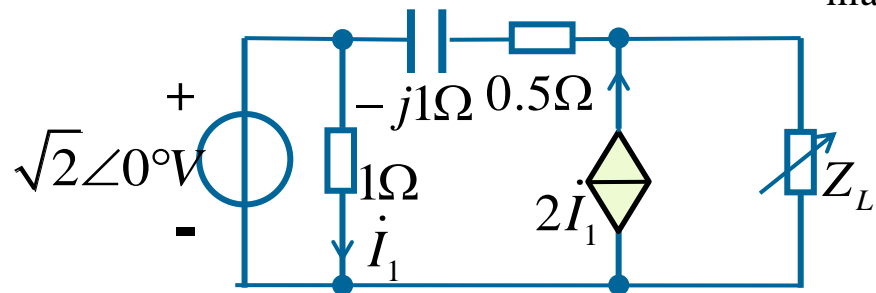
2) 求等效阻抗  $Z_0$ ：

$$Z_0 = (2+2) // j4 = \frac{4\angle 90^\circ}{\sqrt{2}\angle 45^\circ} = 2 + j2\Omega$$

3) 当 $Z_L = Z_0^* = 2 - j2\Omega$ 时，最大功率为：

$$P_{\max} = \frac{U_{oc}^2}{4R_0} = \frac{(4\sqrt{2})^2}{4 \times 2} = 4\text{ W}$$

8-30 电路如题图7-30所示，试求负载  $Z_L$  为何值时可获得最大功率？最大功率  $P_{\max}$  为多少？



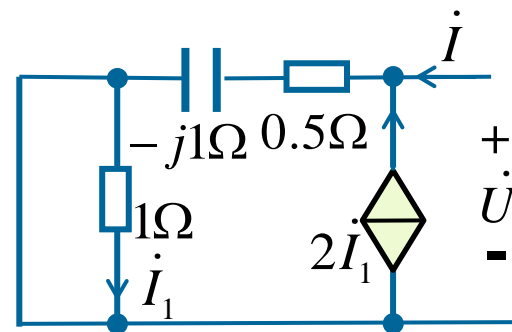
解：  $\dot{U}_{oc} = 2\dot{I}_{10}(0.5 - j1) + \sqrt{2} \angle 0^\circ$

$$\dot{I}_{10} = \frac{\sqrt{2} \angle 0^\circ}{1} = \sqrt{2} \angle 0^\circ \text{ A}$$

$$\therefore \dot{U}_{oc} = 2\sqrt{2} - j2\sqrt{2} = 4 \angle -45^\circ \text{ V}$$

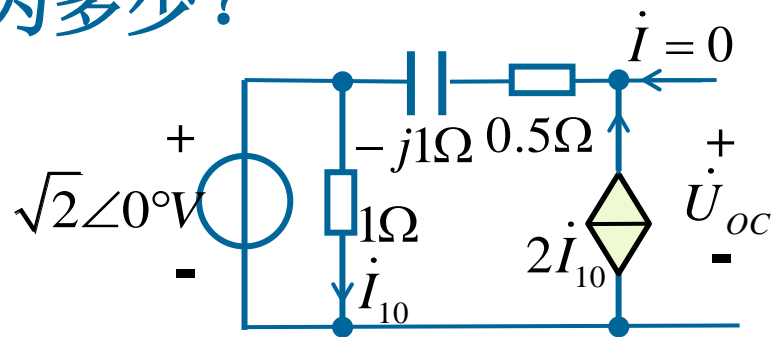
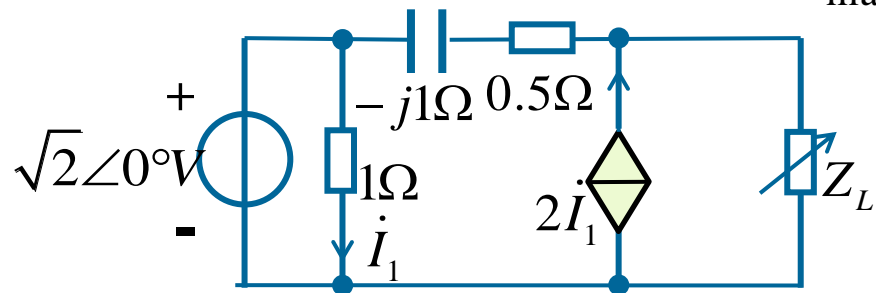
$$\dot{I}_1 = 0 \text{ A} \Rightarrow 2\dot{I}_1 = 0 \quad \therefore Z_0 = 0.5 - j1\Omega$$

当  $Z_L = Z_0 = 0.5 + j1\Omega$  时，可获得最大功率： $P_{\max} = \frac{U_{oc}^2}{4R_0} = 8\text{W}$





8-30 电路如题图7-30所示，试求负载  $Z_L$  为何值时可获得最大功率？最大功率  $P_{\max}$  为多少？



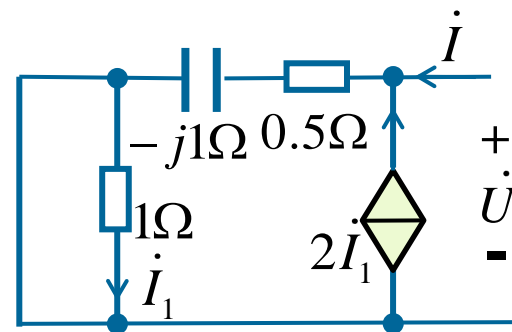
解：  $\dot{U}_{oc} = 2\dot{I}_{10}(0.5 - j1) + \sqrt{2} \angle 0^\circ$

$$\dot{I}_{10} = \frac{\sqrt{2} \angle 0^\circ}{1} = \sqrt{2} \angle 0^\circ \text{ A}$$

$$\therefore \dot{U}_{oc} = 2\sqrt{2} - j2\sqrt{2} = 4 \angle -45^\circ \text{ V}$$

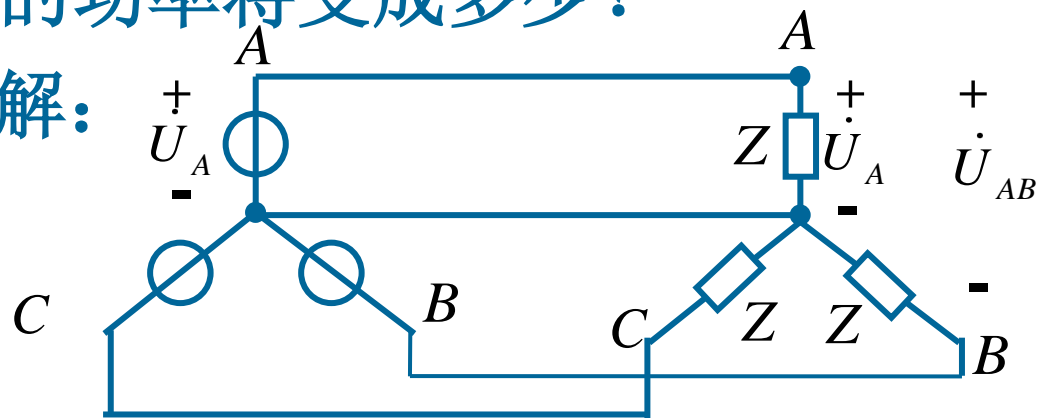
$$\dot{I}_1 = 0 \text{ A} \Rightarrow 2\dot{I}_1 = 0 \quad \therefore Z_0 = 0.5 - j1\Omega$$

当  $Z_L = Z_0 = 0.5 + j1\Omega$  时，可获得最大功率： $P_{\max} = \frac{U_{oc}^2}{4R_0} = 8\text{W}$



**8-31** 已知三相电路中星形连接的三相负载每相阻抗  $Z = 12 + j16\Omega$ ，接至对称三相电源，其线电压为**380V**。若端线阻抗忽略不计，试求线电流及负载吸收的功率；若将此三相负载改为三角形连接，线电流及负载吸收的功率将变成多少？

解：



$$\dot{U}_{AB} = 380 \angle 0^\circ \text{V}$$

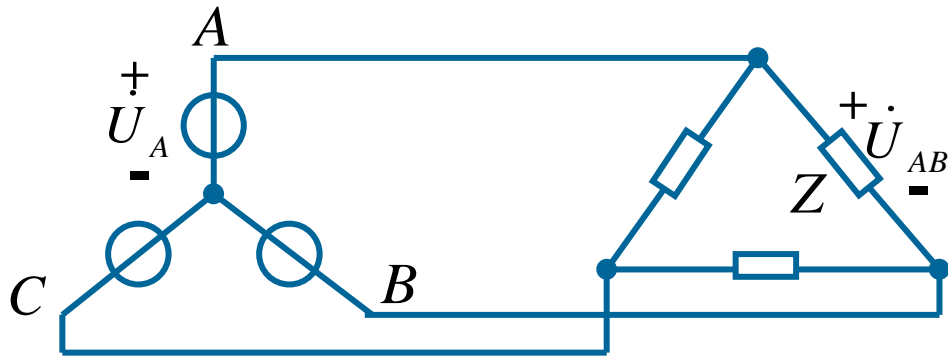
$$\dot{U}_A = \frac{1}{\sqrt{3}} \dot{U}_{AB} \angle -30^\circ$$

$$= 220 \angle -30^\circ \text{V}$$

$$\dot{I}_A = \frac{\dot{U}_A}{Z} = \frac{220 \angle -30^\circ}{12 + j16} = \frac{220 \angle -30^\circ}{20 \angle 53.1^\circ} = 11 \angle -83.1^\circ \text{A}$$

$$\therefore I_l = I_P = 11 \text{A}$$

$$P = 3U_P I_P \cos \theta_Z = 3 \times 220 \times 11 \times \cos 53.1^\circ = 4356 \text{W}$$



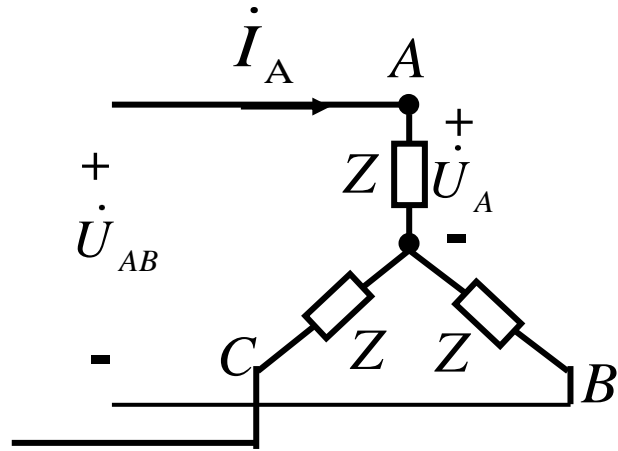
$$\dot{U}_{AB} = 380 \angle 0^\circ \text{V}$$

$$\dot{I}_{AB} = \frac{\dot{U}_{AB}}{Z} = \frac{380 \angle 0^\circ}{12 + j16} = \frac{380 \angle 0^\circ}{20 \angle 53.1^\circ} = 19 \angle -53.1^\circ \text{A}$$

$$I_P = 19 \text{A} = \frac{1}{\sqrt{3}} I_l \Rightarrow I_l = 32.9 \text{A}$$

$$P = 3U_P I_P \cos \theta_Z = 3 \times 380 \times 19 \times \cos 53.1^\circ = 12996 \text{W}$$

## 8-32



由题意可知  $\dot{U}_{AB} = 380 \angle 60^\circ \text{V}$

星形连接A相负载相电压  $\dot{U}_A = \frac{1}{\sqrt{3}} \dot{U}_{AB} \angle -30^\circ = 220 \angle 30^\circ \text{V}$

A相负载相电流  $\dot{I}_A = \frac{\dot{U}_A}{Z} = \frac{220 \angle 30^\circ}{3 + 4j} = 44 \angle -23.1^\circ \text{A}$

根据对称三相电路对称性

$$\dot{I}_B = 44 \angle -23.1^\circ - 120^\circ = 44 \angle -143.1^\circ \text{A}$$

$$\dot{I}_C = 44 \angle -23.1^\circ + 120^\circ = 44 \angle 96.9^\circ \text{A}$$

$$P = 3U_p I_p \cos \theta_Z = 3 \times 220 \times 44 \times \cos 53.1^\circ = 17424 \text{W}$$

$$i_A(t) = 44\sqrt{2} \cos(314t - 23.1^\circ) \text{A}$$

$$i_B(t) = 44\sqrt{2} \cos(314t - 143.1^\circ) \text{A}$$

$$i_C(t) = 44\sqrt{2} \cos(314t + 96.9^\circ) \text{A}$$

8-41 题图7-41所示二端网络N的端口电流、电压分别为

$$i(t) = 5 \cos t + 2 \cos\left(2t + \frac{\pi}{4}\right) \text{A},$$
$$u(t) = 3 + \cos\left(t + \frac{\pi}{2}\right) + \cos\left(2t - \frac{\pi}{4}\right) + \cos\left(3t - \frac{\pi}{3}\right) \text{V}$$

试求网络吸收的平均功率。

解：

$$P = \sum_{k=0}^3 U_k I_k \cos \theta_{zk}$$
$$= U_0 I_0 + U_1 I_1 \cos \frac{\pi}{2} + U_2 I_2 \cos\left(-\frac{\pi}{2}\right)$$
$$= 3 \times 0 + \frac{1}{\sqrt{2}} \cdot \frac{5\sqrt{2}}{2} \cos \frac{\pi}{2} + \frac{1}{\sqrt{2}} \cdot \sqrt{2} \cos\left(-\frac{\pi}{2}\right) = 0$$

## 8-42 已知流过 $2\Omega$ 电阻的电流

$$i(t) = 2 + 2\sqrt{2} \cos t + \sqrt{2} \cos(2t + 30^\circ) \text{ A},$$

试求电阻消耗的平均功率。

解:

$$P = \sum_{k=0}^2 I_k^2 R$$

$$= (I_0^2 + I_1^2 + I_2^2) R = (2^2 + 2^2 + 1^2) \times 2 = 18 \text{ W}$$